

### CONTROL LOOP MODELING OF L6561-BASED TM PFC

by Claudio Adragna

*This paper provides a model and a tool for evaluating and improving the control loop characteristics of L6561-based PFC preregulators in boost topology and operated in Transition Mode (TM).*

*Such a subject is now becoming topical since TM PFC preregulators are more and more used in systems other than electronic lamp ballast where the input voltage range is limited and the load current is almost constant.*

*The ability to operate under large variations of both input voltage and load current, as well as the use of TM PFC systems as preregulators for switching converters, requires a more accurate design of the control loop. The goal will be not only to ensure a narrow bandwidth in order to achieve a high Power Factor, but also to have enough phase margin so as to make sure the system is stable over a large range of operating conditions.*

#### INTRODUCTION

PFC preregulators based on the boost topology working in Transition Mode (TM, see fig. 1) have been widespread in electronic lamp ballast systems. This kind of equipment almost always works under a single mains supply (110 or 220 VAC, with some tolerance) and the use of a PFC preregulator is mainly aimed at optimising the downstream half-bridge lamp driver and improving their inherent extremely poor PF.

The PFC preregulator sees the downstream stage as a constant load, so it is requested to work under a limited range of operating conditions. From the control loop standpoint, this means that the frequency compensation of the error amplifier can be very simple, typically just a feedback capacitor. Its capacitance will be high enough to ensure the crossover frequency of the open loop gain is low, so as to achieve a high PF (see Ref. [1]).

**Figure 1. Typical L6561-based TM PFC preregulator**

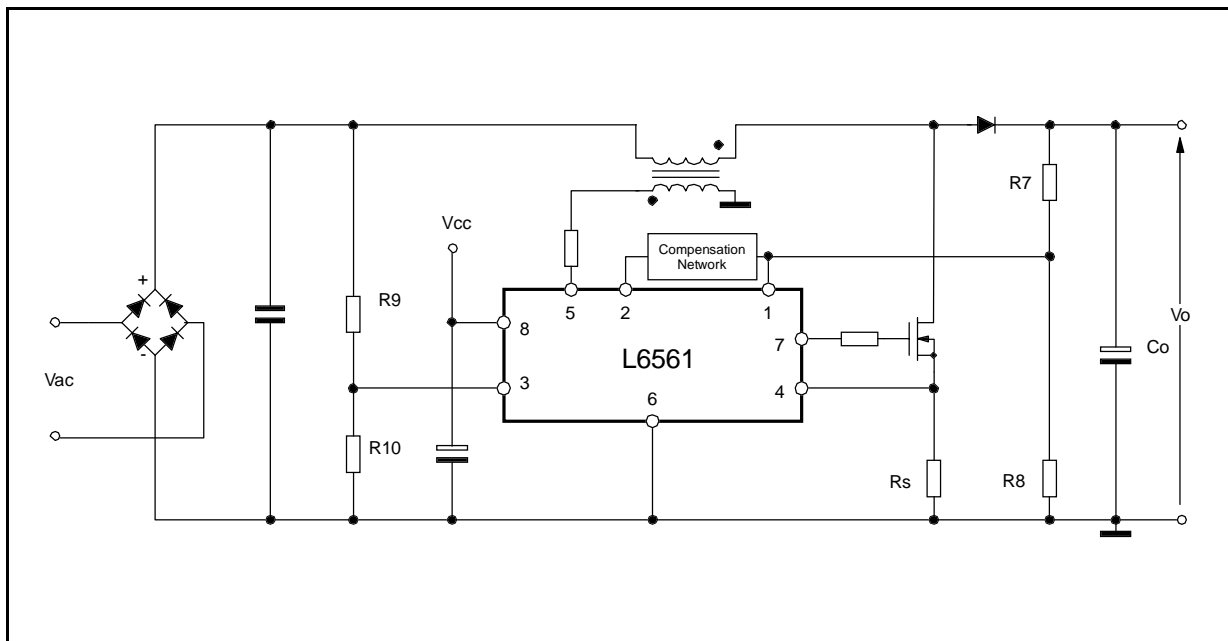




Fig. 3 illustrates how the various blocks of fig. 2 relate with the electrical circuit, both external and inside the L6561. For details on the internal circuit and its operation please refer to Ref. [1].

The loop gain of PFC preregulators must have a very low crossover frequency ( $f_c$ ) so as to maintain  $V_{COMP}$  (Error Amplifier output) fairly constant over a given line cycle and ensure a high PF.

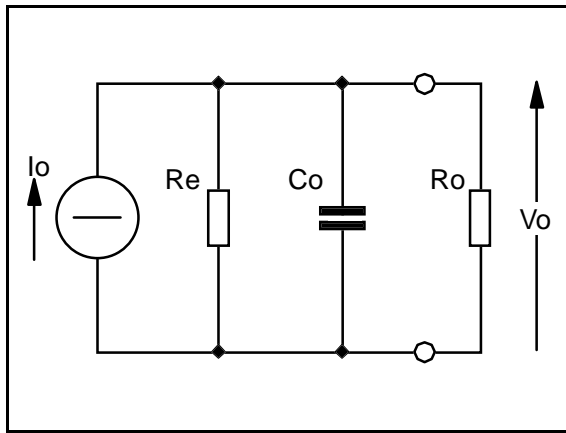
As a rule of thumb,  $f_c$  should not exceed 20-25 Hz at maximum mains voltage.

This allows to assume that the control action takes place on the peak amplitude (or, which is the same, the RMS value) of the various quantities inside the loop.

The first step is to determine the transfer function of the power stage,  $G_4(s)$ , defined as:

$$G_4(s) = \frac{dV_o}{dI_{Lpk}} = \frac{dV_o}{dI_o} \cdot \frac{dI_o}{dI_{Lpk}}$$

**Figure 4. Power stage model,  $G_4(s)$**



where  $V_o$  is the DC output voltage,  $I_o$  the DC output current and  $I_{Lpk}$  is the peak value of the inductor current.

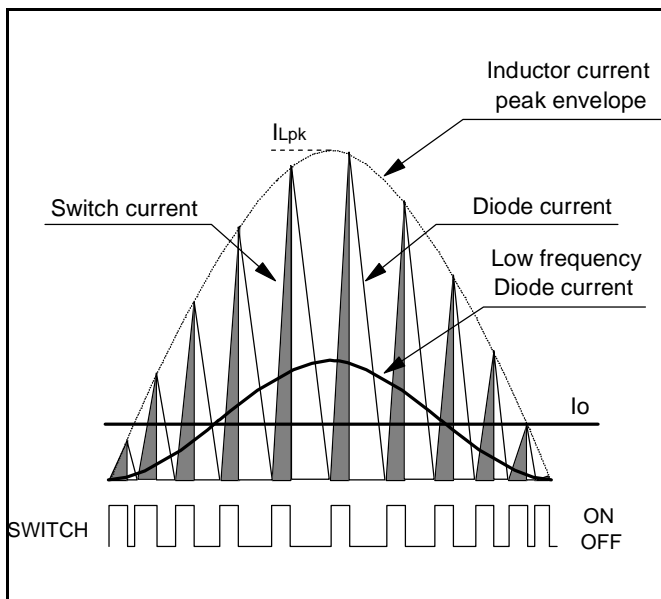
Under the above assumption, the power stage can be modeled as illustrated in fig. 4: a controlled current source (with a shunt resistor  $R_e$ ) that drives the output bulk capacitor  $C_o$  and the load resistance  $R_o$  ( $= V_o / I_o$ ). The zero due to the ESR associated with  $C_o$  is far beyond the crossover frequency thus it is neglected.

The current source can be characterised with the following considerations: the low frequency component of the boost diode current is found by averaging the discharge portion of the inductor current (the white triangles of fig. 5) over a given switching cycle.

The low frequency current, averaged over a mains half-cycle yields the DC output current  $I_o$ :

$$I_o = \frac{1}{2} \cdot (1 - D) \cdot I_{Lpk} \cdot \sin \theta = \frac{1}{2} \cdot \frac{\sqrt{2} \cdot V_{rms} \cdot \sin \theta \cdot I_{Lpk} \cdot \sin \theta}{V_o} = \frac{\sqrt{2}}{4} \cdot \frac{V_{rms} \cdot I_{Lpk}}{V_o}$$

**Figure 5. Boost PFC currents**



where  $D$  is the switch duty cycle,  $\theta$  is the instantaneous phase angle of the mains voltage and  $V_{rms}$  its effective (RMS) value.

The AC model illustrated in fig. 4 can be found by calculating the total differential of the above expression of  $I_o$ . A few algebraic manipulations would show that the shunt resistor  $R_e$  always equals the DC load resistance  $R_o$ , thus it changes depending on the power delivered by the system. Now it is necessary to consider two separate cases.

If the load is purely resistive (or equivalent to a resistor, like in the case of a lamp ballast circuit), the AC load resistance equals  $R_o$ . The parallel of this resistance with  $R_e$ , combined with the output bulk capacitor, gives origin to a pole located at:

$$\omega_p = \frac{2}{R_o \cdot C_o}$$

which is usually in the range of 1 to 5 Hz.

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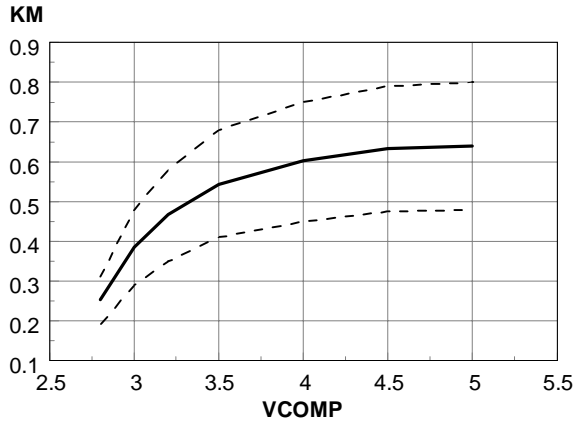
In case the PFC preregulator provides a DC bus supplying a downstream switching converter, the load should be regarded as a "constant power" load rather than a resistor. In fact, as long as a switching converter is in regulation, the power it demands of the source is practically independent of the input voltage (converter's efficiency changes very little).

In this case, the AC load resistance is equal to  $-R_o$  (if the DC bus decreases the current demanded of the PFC increases, whence the negative sign). As a result, the parallel combination with  $R_e$  tends to infinity and the two resistances cancel. The current source drives only the output capacitor and the pole location tends to zero. In the end,  $G4(s)$  will be given by:

$$G4(s) = \begin{cases} \frac{\sqrt{2}}{8} \cdot \frac{V_{irms}}{V_o} \cdot \frac{R_o}{1 + s \cdot \frac{R_o \cdot C_o}{2}} & \text{(resistive load)} \\ \frac{\sqrt{2}}{4} \cdot \frac{V_{irms}}{V_o} \cdot \frac{1}{s \cdot C_o} & \text{(constant power load)} \end{cases}$$

The gain of the PWM modulator,  $G3$ , which includes the current loop, is simply:

**Figure 6. Plot of  $K_M$  vs.  $E/A$  output**



$$G3 = \frac{dI_{Lpk}}{dV_{cspk}} = \frac{1}{R_s}$$

where  $R_s$  is the sense resistor connected between the source of the external MOSFET and ground (across which the L6561 reads the inductor current through pin 3).

To calculate the transfer function  $G2$  of the multiplier block, one can consider that a variation  $\Delta V_{COMP}$ , due to a line and/or load change, modifies the peak amplitude  $V_{cspk}$  of the rectified sinusoid at the output of the multiplier. Therefore:

$$G2 = \frac{dV_{cspk}}{dV_{COMP}} = K_M \cdot K_P \cdot \sqrt{2} \cdot V_{irms}$$

where  $K_M$  is the gain of the multiplier and  $K_P$  the partition ratio of the resistor divider that feeds a portion of the input voltage into pin 3.

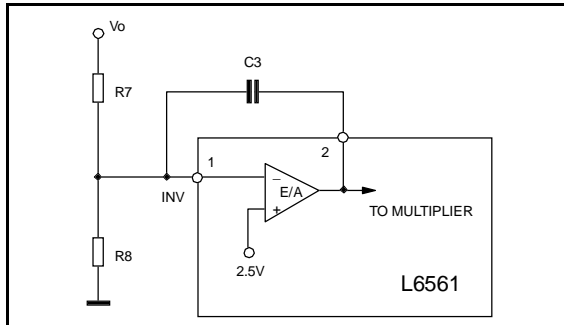
The electrical characteristics of the L6561 specify  $K_M = 0.6 \pm 25\%$  (@  $V_{COMP} = 4V$ , including temperature) but actually  $K_M$  decreases for low values of  $V_{COMP}$ . In fig. 6 the typical value of  $K_M$  is plotted against  $V_{COMP}$  along with the tolerance limits. Since  $V_{COMP}$  gets lower when the mains voltage is high, this variation of  $K_M$  partly compensates for the increase of  $G2$  with  $V_{irms}$ , thus providing a mild voltage feedforward effect.

If one wants to take this non-linearity into account, he or she should linearise the large-signal multiplier gain in the neighborhood of the quiescent point of the error amplifier, so as to get the small-signal gain ( $k_m$ ). Please refer to [1] and the Appendix for the relevant calculation technique.

Ultimately, the control-to-output transfer function will be:

$$G(s) = \frac{dV_o}{dV_{COMP}} = G2 \cdot G3 \cdot G4(s) = \begin{cases} \frac{1}{4} \cdot \frac{k_m \cdot K_P \cdot V_{irms}^2}{V_o} \cdot \frac{R_o}{R_s} \cdot \frac{1}{1 + s \cdot \frac{R_o \cdot C_o}{2}} & \text{(resistive load)} \\ \frac{1}{2} \cdot \frac{k_m \cdot K_P \cdot V_{irms}^2}{R_s \cdot V_o} \cdot \frac{1}{s \cdot C_o} & \text{(constant power load)} \end{cases}$$

where the small-signal multiplier gain  $k_m$  could be assumed equal to  $K_M$  for simplicity.

**Figure 7. Typical compensation scheme in PFC preregulators for lamp ballast**

From the above equations, it is apparent that the gain of the control-to-output function is strongly dependent on the input voltage, despite the slight compensation provided by  $K_M$ . For design purpose,  $G(s)$  will have to be considered at the maximum mains voltage, where the gain is maximum and the loop bandwidth is maximum as well.

The feedback block is usually made up of a simple resistor divider (see fig. 7). Only the upper resistor R7 is significant to the loop gain (the lower resistor R8 just sets the value of  $V_o$ ). It is then convenient to assume  $H=1$  and to consider R7 as a part of the error amplifier block  $G_1(s)$ .

### Error Amplifier Compensation

In PFC preregulators that supply an electronic lamp ballast the error amplifier is compensated typically as shown in fig. 7 (see also Ref. [2] and [3]).

For this kind of load this circuit gives satisfactory results. It may not be acceptable, however, in other systems where stability must be ensured over a wide range of input voltage and load current, and does not work at all when the PFC preregulator supplies a switching converter.

Figure 8 shows the suggested compensation schemes for both the cases under consideration.

With a resistive load the loop can be stabilised by adding a pole in the origin plus a low frequency zero that compensates the pole of the control-to-output gain (network a). Ideally, this can give the desired bandwidth with  $90^\circ$  phase margin as well as high DC gain for good load regulation.

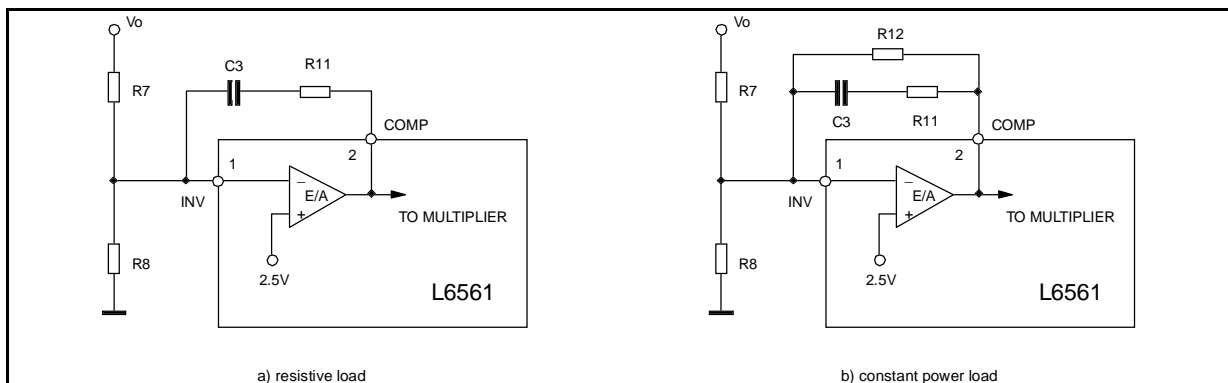
With a constant power load the control-to-output gain has a pole in the origin thus the DC gain of the error amplifier should be externally limited with a feedback resistor. If not, a second pole in the origin would be introduced, which would result in a system whose stability might be critical.

Limiting the gain goes to the detriment of preregulator's load regulation but this has not a serious impact on the overall system since the downstream converter will easily compensate for that.

The compensation network (b) adds a pole-zero couple that both makes the gain roll off at low frequency (so as to cross the 0 dB axis at low frequency) and boosts the phase in the neighborhood of the cross-over frequency (so as to increase phase margin).

The transfer functions of the compensation networks of fig. 8 a) and b) are respectively:

$$G_1(s) = \frac{dV_{COMP}}{dV_o} = \begin{cases} \frac{1 + s \cdot C_3 \cdot R_{11}}{s \cdot C_3 \cdot R_7} & \text{(circuit a – resistive load)} \\ \frac{R_{12}}{R_7} \cdot \frac{1 + s \cdot C_3 \cdot R_{11}}{1 + s \cdot C_3 \cdot (R_{11} + R_{12})} & \text{(circuit b – constant power load)} \end{cases}$$

**Figure 8. Suggested compensation networks for TM boost PFC**

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As a tool to ease the design of L6561's E/A compensation networks in TM boost PFC preregulators, the Appendix contains a Mathcad® file gathering the theory above illustrated and performing all the necessary calculations.

### Conclusions

This paper gets an insight into the control loop of TM controlled Boost PFC preregulators based on the L6561 PFC controller. This reveals that the simple feedback capacitor used to compensate the error amplifier in preregulators for lamp ballast may not be adequate in systems that may experience large variations in input voltage and/or load current. Moreover it leads to an unstable loop if the load is a switching converter. Appropriate compensation schemes are suggested for both cases and a calculation tool (Mathcad® file) is provided so as to make control loop design easier in such systems.

### References

- [1] "L6561, Enhanced Transition Mode Power Factor Corrector", (AN966)
- [2] "L6569 - L6561 Lighting Application with PFC" (AN991)
- [3] "Electronic Ballast with PFC Using L6574 and L6561" (AN993)
- [4] "Design Equations of High-Power-Factor Flyback Converters Based on the L6561" (AN1059)
- [5] "Flyback Converters with the L6561 PFC Controller" (AN1060)

### Appendix

This Mathcad® file allows to design the control loop and performs a stability analysis of PFC preregulators in boost topology operated in Transition Mode and controlled by the L6561.

Highlighted equations indicate data that must be manually entered. These data are supposed to be known to the user as a result of the design of the PFC preregulator (the use of the PFC design software included in the CD-ROM "Linear and Switching Voltage Regulators" is recommended). The example values are taken from the L6561 demo board circuit.

#### PFC Converter Data:

Output Voltage	$V_o := 400$	V
Output Capacitor	$C_o := 47$	$\mu\text{F}$
Sense Resistor	$R_s := 0.41$	$\Omega$
Output Overvoltage Threshold	$\text{OVP} := 40$	V
Expected Efficiency	$\eta := 0.9$	

#### Multiplier Biasing:

Input Divider Upper Resistor	$R_{up} := 1240$	$\text{k}\Omega$
Input Divider Lower Resistor	$R_{low} := 10$	$\text{k}\Omega$

#### Analysis Setpoint:

Mains RMS Voltage	$V_{rms} := 264$	V
Output Power	$P_o := 80$	W

**Preliminary calculations & Service Variables:**

Equivalent Load Resistance  $R_o := \frac{V_o^2}{P_o}$   $R_o = 2 \cdot 10^3$   $\Omega$

Input Divider Gain  $KP := \frac{R_{low}}{R_{low} + R_{up}}$   $KP = 8 \cdot 10^{-3}$

Large-signal Multiplier Gain:  $KM(V_{COMP}) := 0.651 \cdot (1 - 85.29 \cdot e^{-1.776 \cdot V_{COMP}})$

Error Amplifier Quiescent Point:  $V_{COMP} := 4$

$$V_{COMP} := \text{root} \left( 2.5 + \frac{2 \cdot P_o \cdot R_s}{\eta \cdot KM(V_{COMP}) \cdot KP \cdot V_{irms}^2} - V_{COMP}, V_{COMP} \right)$$

$V_{COMP} = 2.898$  [V]

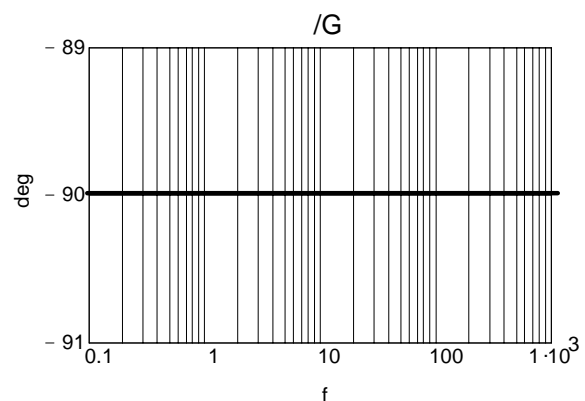
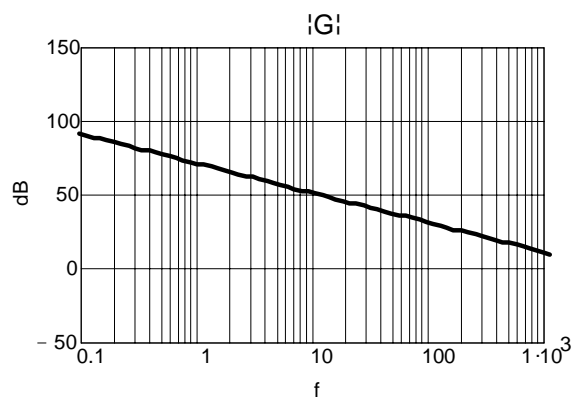
Small signal Multiplier Gain  $km := \frac{d}{dV_{COMP}} [KM(V_{COMP}) \cdot (V_{COMP} - 2.5)]$

$km = 0.557$

$j := \sqrt{-1}$   $n := 100$   $\text{Dec} := 6$   $w := 0, 1..n$   $\omega(w) := 10^{w \cdot \frac{\text{Dec}}{n} - 1}$   $f := 1$

**Control-to-Output Transfer Function (constant power load):**

$$G(\omega) := \frac{km \cdot KP \cdot V_{irms}^2}{2 \cdot V_o} \cdot \frac{1}{R_s} \cdot \frac{10^6}{j \cdot \omega \cdot C_o}$$



**Compensated E/A Transfer Function (constant power load, refer to fig.8b)**

DC gain ( $\Delta V_o / \Delta V_{COMP}$ ):

$G_o := 0.30$

Pole:

$p := 0.23$

Hz

Zero:

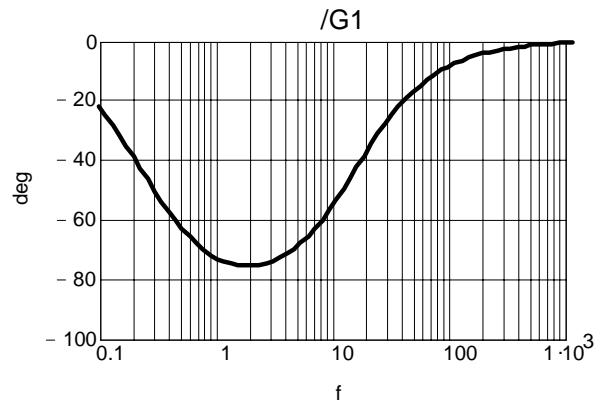
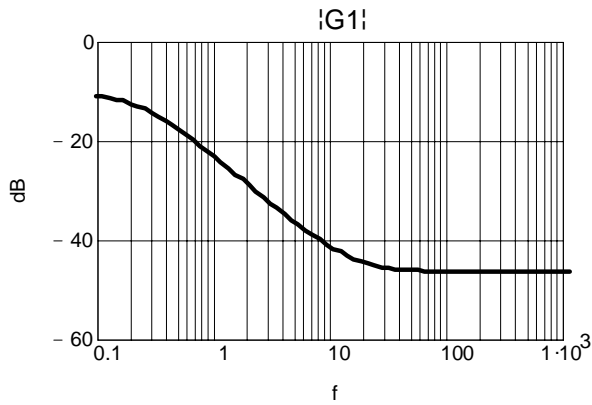
$z := 15$

Hz

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Transfer Function:

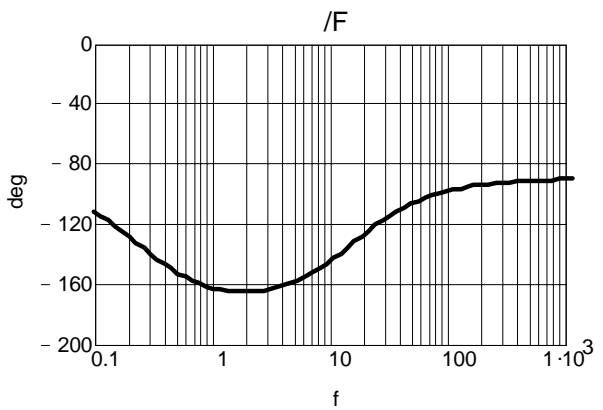
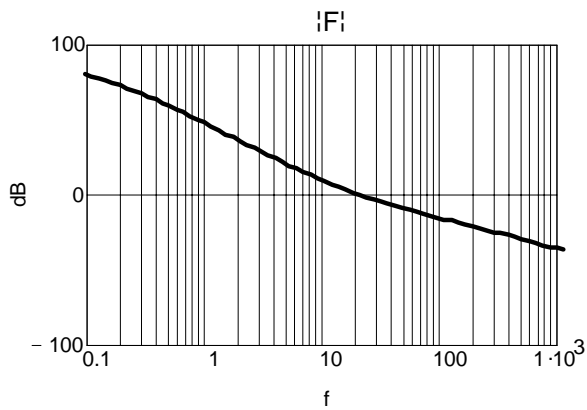
$$G1(\omega) := G_O \cdot \frac{1 + j \cdot \frac{\omega}{2 \cdot \pi \cdot z}}{1 + j \cdot \frac{\omega}{2 \cdot \pi \cdot p}}$$



Open Loop Transfer Function (constant power load):

$$F(\omega) := G(\omega) \cdot G1(\omega)$$

$$\Phi F(\omega) := \arg(F(\omega)) \cdot \frac{180}{\pi}$$



Crossover Frequency:

$$f_c := |\text{root}(|F(2 \cdot \pi \cdot f)| - 1, f)|$$

$$f_c = 18.836$$

Hz

Phase Margin:

$$\Phi := 180 + \Phi F(2 \cdot \pi \cdot f_c)$$

$$\Phi = 52.167$$

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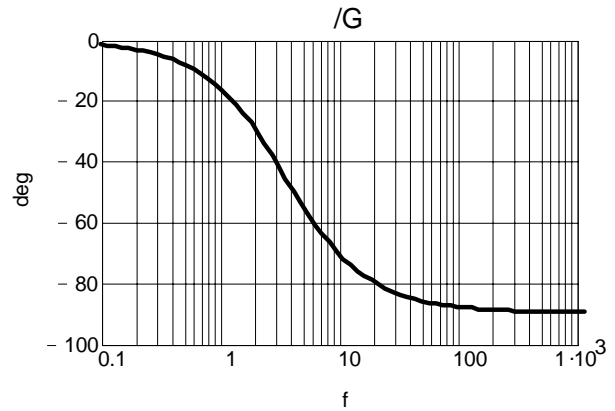
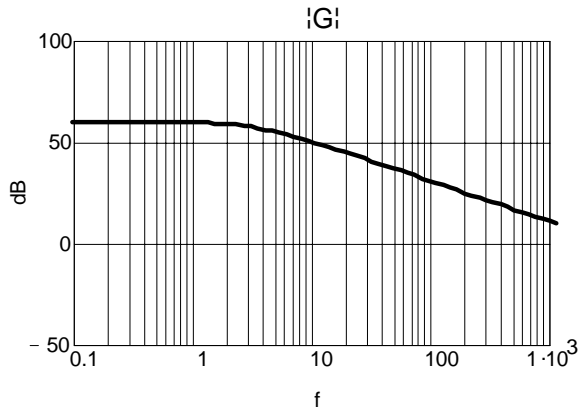


### Feedback Network Implementation (constant power load, refer to fig. 8b):

Output Divider Upper Resistor	$R7 = \frac{OVP}{40} \cdot 10^3$		
	$R7 = 1 \cdot 10^3$		kΩ
Output Divider Lower Resistor	$R8 = \frac{2.5}{V_O - 2.5} \cdot R7$	$R8 = 6.289$	kΩ
Parallel Feedback Resistor:	$R12 = G_O \cdot R7$	$R12 = 300$	kΩ
Series Feedback Capacitor	$C3 = \frac{10^6}{2 \cdot \pi \cdot R12} \cdot \left( \frac{1}{p} \cdot \frac{1}{z} \right)$		
	$C3 = 2.271 \cdot 10^3$		nF
Series Feedback Resistor	$R11 = \frac{10^6}{2 \cdot \pi \cdot z \cdot C3}$	$R11 = 4.672$	kΩ

### Control-to-Output Transfer Function (resistive load):

$$G(\omega) := \frac{k_m \cdot K_P \cdot V_{irms}^2}{4 \cdot V_O} \cdot \frac{R_O}{R_s} \cdot \frac{1}{1 + j \cdot \omega \cdot C_O \cdot \frac{R_O}{2} \cdot 10^{-6}}$$



Pole Location:	$p := \frac{10^6}{\pi \cdot R_O \cdot C_O}$	$p = 3.386$	Hz
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### Compensated E/A Transfer Function (resistive Load, refer to fig. 8a):

High Frequency Gain:

$$G_h := 0.005$$

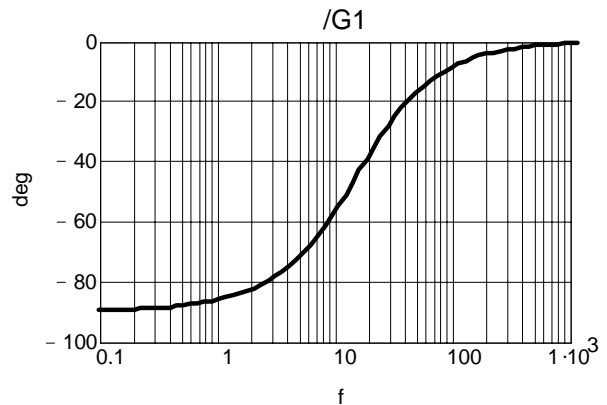
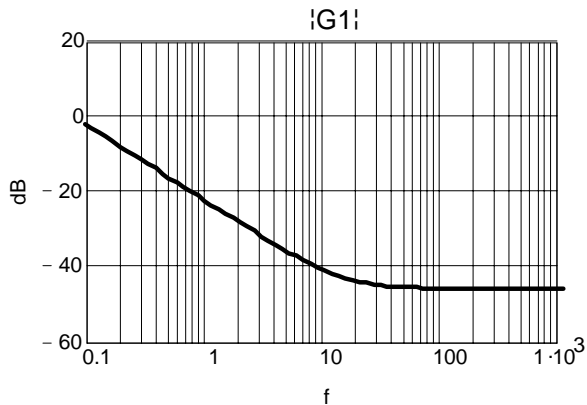
Zero:

$$z := 15$$

Hz

Transfer Function:

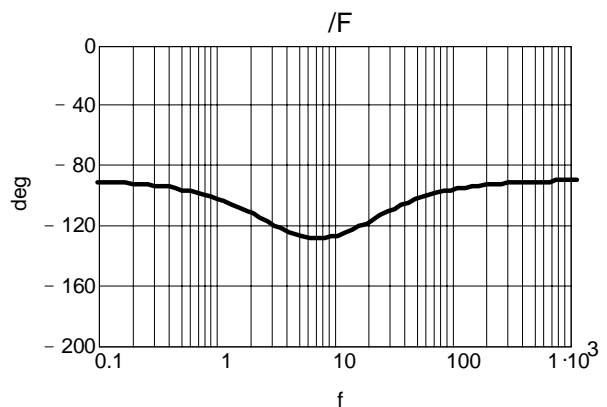
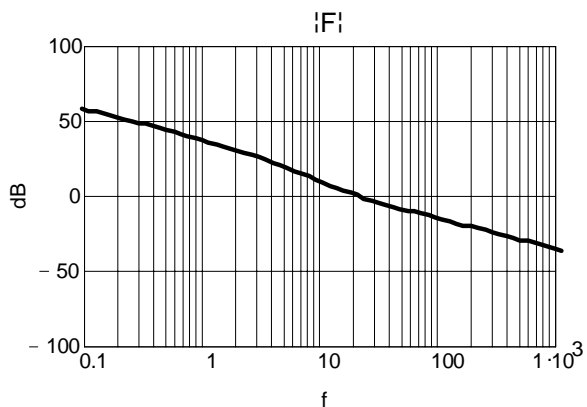
$$G1(\omega) := G_h \cdot 2 \cdot \pi \cdot z \cdot \frac{1 + j \cdot \frac{\omega}{2 \cdot \pi \cdot z}}{j \cdot \omega}$$



### Open Loop Transfer Function (resistive load)

$$F(\omega) := G(\omega) \cdot G1(\omega)$$

$$\Phi F(\omega) := \arg(F(\omega)) \cdot \frac{180}{\pi}$$



Crossover Frequency:

$$f_c := \text{root}(|F(2 \cdot \pi \cdot f)| - 1, f)$$

$$f_c = 19.805$$

Hz

Phase Margin:

$$\Phi := 180 + \Phi F(2 \cdot \pi \cdot f_c)$$

$$\Phi = 62.563$$

°

**Feedback Network Implementation (resistive load, refer to fig. 8a):**

Equivalent Load Resistance

$$R7 := \frac{OVP}{40} \cdot 10^3$$

$$R7 = 1 \cdot 10^3$$

kΩ

Output Divider Lower Resistor

$$R8 := \frac{2.5}{V_O - 2.5} \cdot R7$$

$$R8 = 6.289$$

kΩ

Series Feedback Capacitor

$$C3 := \frac{10^6}{2 \cdot \pi \cdot Z \cdot Gh \cdot R7}$$

$$C3 = 2122 \cdot 10^3$$

nF

Series Feedback Resistor

$$R11 := \frac{10^6}{2 \cdot \pi \cdot Z \cdot C3}$$

$$R11 = 5$$

kΩ

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