Ott: Tool Support for Semantics
User Guide
version 0.10.16

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1 Introduction

Ott is a tool for writing definitions of programming languages and calculi. It takes as input a definition of a language syntax and semantics, in a concise and readable ASCII notation that is close to what one would write in informal mathematics. It generates output:

1. a LaTeX source file that defines commands to build a typeset version of the definition;
2. a Coq version of the definition;
3. a HOL version of the definition;
4. an Isabelle version of the definition;
5. an OCaml version of the syntax of the definition.

Additionally, it can be run as a filter, taking a LaTeX/Coq/Isabelle/HOL/OCaml source file with embedded (symbolic) terms of the defined language, parsing them and replacing them by typeset terms.

This document is a user guide for the tool. The paper

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gives an overview of the project, including discussion of motivation, design decisions, and related work, and one should look at that together with this manual. The project web page

> `http://www.cl.cam.ac.uk/users/pes20/ott/`

includes source and binary distributions of the tool, under a BSD-style licence. It also has a range of examples, including untyped and simply typed CBV lambda calculus, ML polymorphism, various first-order systems from Pierce's TAPL [Pie02], the POPLmark $F_{<:}$ language [ABF+05], a module system by Leroy [Ler96, §4] (extended with a term language and an operational semantics), the LJ Java fragment and LJAM Java module system [SSP07], and a substantial fragment of OCaml.

Our main goal is to support work on large programming language definitions, where the scale makes it hard to keep a definition internally consistent, and hard to keep a tight correspondence between a definition and implementations. We also wish to ease rapid prototyping work with smaller calculi, and to make it easier to exchange definitions and definition fragments between groups. Most simply, the tool can be used to aid completely informal LaTeX mathematics. Here it permits the definition, and terms within proofs and exposition, to be written in a clear, editable, ASCII notation, without LaTeX noise. It generates good-quality typeset output. By parsing (and so sort-checking) this input, it quickly catches a range of simple errors, e.g. inconsistent use of judgement forms or metavariable naming conventions. That same input, extended with some additional data, can be used to generate formal definitions for Coq, HOL, and Isabelle. It should thereby enable a smooth transition between use of informal and formal mathematics. Further, the tool can automatically generate definitions of functions for free variables, single and multiple substitutions, subgrammar checks (e.g. for value subgrammars), and binding auxiliary functions. Ott supports a 'fully concrete' representation, sufficient for many examples but not dealing with general alpha equivalence. An experimental Coq backend generates definitions in locally-nameless style for a subset of the Ott metalanguage. The OCaml backend generates type definitions that may be useful for developing a complete implementation of the language, together with the functions listed above. It does not generate anything for inductively defined relations (the various proof-assistant code extraction facilities can sometimes be used for that). Our focus here is on the problem of writing and editing language definitions, not (directly) on aiding mechanized proof of metatheory. If one is involved in hard proofs about a relatively stable small calculus then it will aid only a small part of the work (and one might choose instead to work just within a single proof assistant), but for larger languages the definition is a more substantial problem — so much so that only a handful of full-scale languages have been given complete definitions. We aim to make this more commonplace, less of a heroic task.

2 Getting started with Ott

This is an alpha release of the Ott tool. It is a snapshot of the current development state, not polished or stable.

2.1 Directory contents

The source distribution contains:

`doc/`	the user guide, in html, pdf, and ps
`emacs/`	an Ott Emacs mode
`tex/`	auxiliary files for LaTeX
`coq/`	auxiliary files for Coq
`hol/`	auxiliary files for HOL
`tests/`	various small example Ott files
`examples/`	some larger example Ott files
`src/`	the (OCaml) Ott sources
`bin/`	the Ott binary (binary distro only)
`Makefile`	a Makefile for the examples
`LICENCE`	the BSD-style licence terms
`README`	this file (Section 2 of the user guide)
`ocamlgraph-0.99a.tar.gz`	a copy of the `ocamlgraph` library

The windows binary distribution omits the OCaml source files and `ocamlgraph` library, and adds a windows binary in the `bin/` directory.

2.2 To build

Ott depends on OCaml version 3.09.1 or later. In particular, Ott cannot be compiled with OCaml 3.08. It also touched an OCaml bug in 3.10.0 for amd64, fixed in 3.10.1.

The command

```
make world-opt
```

builds the `ott` binary in the `bin/` subdirectory.

This will compiles Ott using `ocamlopt`. To force it to compile with `ocamlc` (which may give significantly slower execution of Ott), do "`make world`".

2.3 To run

Ott runs as a command-line tool. Executing `bin/ott` shows the usage and options. To run Ott on the test file `tests/test10.ott`, generating LaTeX in `test10.tex` and Coq in `test10.v`, type:

```
bin/ott -tex test10.tex -coq test10.v  tests/test10.ott
```

Isabelle and HOL can be generated with options `-isa test10.thy` and `-hol test10Script.sml` respectively.

The Makefile has various sample targets, "`make tests/test10.out`", "`make test7`", etc. Typically they generate:

`out.tex`	LaTeX source for a definition
`out.ps`	the postscript built from that
`out.v`	Coq source
`outScript.sml`	HOL source
`out.thy`	Isabelle source

from files `test10.ott`, `test8.ott`, etc., in `tests/`.

```
% minimal
metavar termvar, x ::=

grammar
t :: 't_' ::=
  | x             ::  :: Var
  | \ x . t       ::  :: Lam
  | t t'          ::  :: App
  | ( t )         :: S:: Paren
  | { t / x } t'  :: M:: Tsub

v :: 'v_' ::=
  | \ x . t       ::  :: Lam

subrules
  v <:: t

defns
Jop :: '' ::=

 defn
 t1 --> t2 :: ::reduce::''  by


    --------------------------  :: ax_app
    (\x.t12) v2 -->  {v2/x}t12

    t1 --> t1'
    -------------- :: ctx_app_fun
    t1 t --> t1' t

    t1 --> t1'
    -------------- :: ctx_app_arg
    v t1 --> v t1'
```

Figure 1: Source: `test10.0.ott`

2.4 Emacs mode

The file `emacs/ottmode.el` defines a very simple Emacs mode for syntax highlighting of Ott source files. It can be used by, for example, adding the following to your `.emacs`, replacing `PATH` by a path to your Ott `emacs` directory.

```
(setq load-path (cons (expand-file-name "PATH") load-path))
(require 'ottmode)
```

2.5 Copyright information

The `ocamlgraph` library is distributed under the LGPL (from `http://www.lri.fr/~filliatr/ftp/ocamlgraph/`); we include a snapshot for convenience. For its authorship and copyright information see the files therein.

All other files are distributed under the BSD-style licence in `LICENCE`.

3 A minimal Ott source file: the untyped CBV lambda calculus

Fig. 1 shows an Ott source file for an untyped call-by-value (CBV) lambda calculus. This section explains the basic features that appear there, while in the following sections we show what must be added to generate typeset output, proof assistant definitions, and other things. The figure is colourised, with Ott

keywords like **this** and Ott symbols such as | and ::. Other user-specific input appears like this.

At the top of the figure, the **metavar** declaration introduces a sort of *metavariables* termvar (with synonym x), for term variables. The following **grammar** introduces two grammar rules, one for terms, with *nonterminal root* t, and one for values v. This specifies the concrete syntax of object-language terms, the abstract syntax representations for proof-assistant mathematics, and the syntax of symbolic terms to be used in semantic rules.

Each rule has a rule name prefix (e.g. 't_') and then a list of productions. Each production, e.g.

```
| \ x . t        ::   :: Lam
```

specifies a syntactic form as a list of elements, here '\', 'x', '.', and 't', each of which is either a metavariable (the 'x'), a nonterminal (the 't'), or a terminal (\ . ( ) { } / -->). Within productions all elements must be whitespace-separated, so that the tool can deduce which are terminals. In the symbolic terms in the semantic rules below, however, whitespace is required only where necessary. A few terminals have to be quoted (with '') if they appear in a grammar, e.g. to use | as an object-language token, as they are part of the Ott syntax, but they do not have to be quoted at usage points. (If one accidentally omits inter-token whitespace in the grammar, the output of Ott can be surprising. This is best diagnosed by looking at the colourised ASCII or LaTeX output from Ott.)

Metavariables and nonterminals can be formed from the specified metavariable and nonterminal roots by appending a suffix, e.g. the nonterminal t' in the App and Tsub productions.

Between the ::'s is an optional meta flag **M** or **S**. Non-meta productions give rise to clauses of datatype definitions in the Isabelle/Coq/HOL output, whereas meta productions do not. Later, we will see how the user can specify how meta syntax should be translated away when generating proof assistant output. The two flags **M** and **S** are identical except that productions with the latter are admitted when parsing example concrete terms; the **S** tag is thus appropriate for lightweight syntactic sugar, such as productions for parentheses.

Each production has a production name (e.g. t_Lam), composed of the rule name prefix (here t_) and the production name kernel that follows the ::'s (here Lam). The production name is used as a constructor name in the generated Isabelle/Coq/HOL.

The tool supports arbitrary context-free grammars, extended with special constructs for list forms (c.f. §11).

Following the **grammar** in this example is a **subrule** declaration

```
subrules
  v <:: t
```

declaring that the v grammar rule (of values) is a subgrammar of the t rule (of terms). The tool checks that there is in fact a subgrammar relationship, i.e. that for each production of the lower rule there exists a production of the higher rule with corresponding elements (up to the subrule relation). The subrule declaration means that, in the semantic rules below, we will be able to use v's in places where the grammar specifies t's. In the generated Isabelle/Coq/HOL for this example only one free datatype will be generated, for the t rule, while for the v rule we generate an is_v predicate over the t type. Usages of v nonterminals in the semantic rules will have instances of this predicate automatically inserted.

Finally, we give a collection of definitions of inductive relations. In this example there is just one family of definitions (of operational judgements), introduced by the **defns** Jop; it contains just one definition of a relation, called reduce. In general there may be many **defns** blocks, each of which introduces a mutually recursive collection of **defn**s. The relation definition **defn** ... also includes a grammar production specifying how elements of the relation can be written and typeset, here

```
t1 --> t2
```

As in the main grammar, the tokens of this syntax definition in the header must be space-separated, but usages of the syntax generally need not be. Syntax rules for each family of judgements, and for their union, are implicitly generated. The relation definition is given by a sequence of inference rules, each with a horizontal line separating a number of premises from a conclusion, for example as below.

```
t1 --> t1'
-------------- :: ctx_app_arg
v t1 --> v t1'
```

The conclusion must be a symbolic term of the form of the judgement being defined. In simple cases (as here) the premises can be symbolic terms of the form of any of the defined judgements. More generally (see §6) they can be symbolic terms of a user-defined **formula** grammar. Each rule has a name, composed of a definition family prefix (here empty), a definition prefix (here also empty) and a kernel (the `ctx_app_arg`).

The symbolic terms in semantic rules are parsed with a scannerless parser, built using parser combinators over character-list inputs. The parser searches for all parses of the input. If none are found, the ASCII and TeX output are annotated `no parses`, with a copy of the input with `***` inserted at the point where the last token was read. This is often at the point of the error (though if, for example, a putative dot form is read but the two element lists cannot be anti-unified, it will be after the point of the error). If multiple parses are found, the TeX output is annotated `multiple parses` and the different parses are output to the console in detail during the Ott run. If the option `picky_multiple_parses` is set to `true`, multiple parses are always reported. If it set to `false`, a symbolic term is considered ambiguous only if two different parses compile to different strings (for a target). The parser combinators use memoization and continuation-passing to achieve reasonable performance on the small symbolic terms that are typical in semantic rules. Their performance on large (whole-program size) examples is untested. To resolve ambiguity one can add metaproductions for parentheses (as in Fig. 1), or production-name annotations in particular symbolic terms, e.g. the `:t_tsub:` in the `AppAbs` rule of the POPLmark example, `test7.ott`. There is currently no support for precedence or associativity.

This file is included in the distribution as `tests/test10.0.ott`. It can be processed by executing

```
bin/ott tests/test10.0.ott
```

from the main directory. This simply reads in the file, checking that it is well-formed, and echos a colourised version to the screen, with metavariables in red, nonterminals in yellow, terminals in green, and object variables in white. The colourisation uses vt220 control codes; if they do not work on your screen add `-colour false` to the middle of the command line. To suppress the echo of the definition, add `-show_post_sort false` and `-show_defns false`.

3.1 Index variables

In addition to the **metavar** declarations above, the user can declare any number of distinguished *index* metavariables, e.g. by:

```
indexvar index, i, j, n, m ::= {{ isa num }} {{ coq nat }} {{ hol num }}
```

Given such a declaration, `index`, `i`, `j`, `n` and `m` can be used in suffixes, e.g. in the production

```
|  ( t1 , .... , tn )            :: :: Tuple
```

There is a fixed ad-hoc language of suffixes, including numbers, primes, and index variables (see §20). Index metavariables cannot themselves be suffixed.

4 Generating LaTeX

The example from the previous section can already be used to generate LaTeX, for example by executing

```
bin/ott -tex out.tex tests/test10.0.ott
```

to produce a LaTeX file `out.tex`. One often needs to fine-tune the default typesetting, as illustrated in Figure 2 (the Ott source) and Figure 3 (the resulting LaTeX). (The latter was built using the additional option `-tex_show_meta false`, to suppress display of the metaproductions.) The source file has three additions to the previous file. Firstly, the **metavar** declaration is annotated with a specification of how metavariables should be translated to LaTeX:

```
% minimal + latex + comments
metavar termvar, x ::=
  {{ tex \mathit{[[termvar]]} }}

grammar
t :: 't_' ::=                                  {{ com term    }}
  | x             ::  :: Var                     {{ com variable}}
  | \ x . t       ::  :: Lam                     {{ com lambda  }}
  | t t'          ::  :: App                     {{ com app     }}
  | ( t )         :: S:: Paren
  | { t / x } t'  :: M:: Tsub

v :: 'v_' ::=                                  {{ com value   }}
  | \ x . t       ::  :: Lam                     {{ com lambda  }}

terminals :: 'terminals_' ::=
  | \             ::  :: lambda  {{ tex \lambda }}
  | -->           ::  :: red     {{ tex \longrightarrow }}

subrules
  v <:: t

defns
Jop :: '' ::=

 defn
 t1 --> t2 :: ::reduce::'' {{ com [[t1]] reduces to [[t2]]}} by


    ---------------------------  :: ax_app
    (\x.t12) v2 -->  {v2/x}t12

    t1 --> t1'
    -------------- :: ctx_app_fun
    t1 t --> t1' t

    t1 --> t1'
    -------------- :: ctx_app_arg
    v t1 --> v t1'
```

Figure 2: Source: `test10.2.ott`

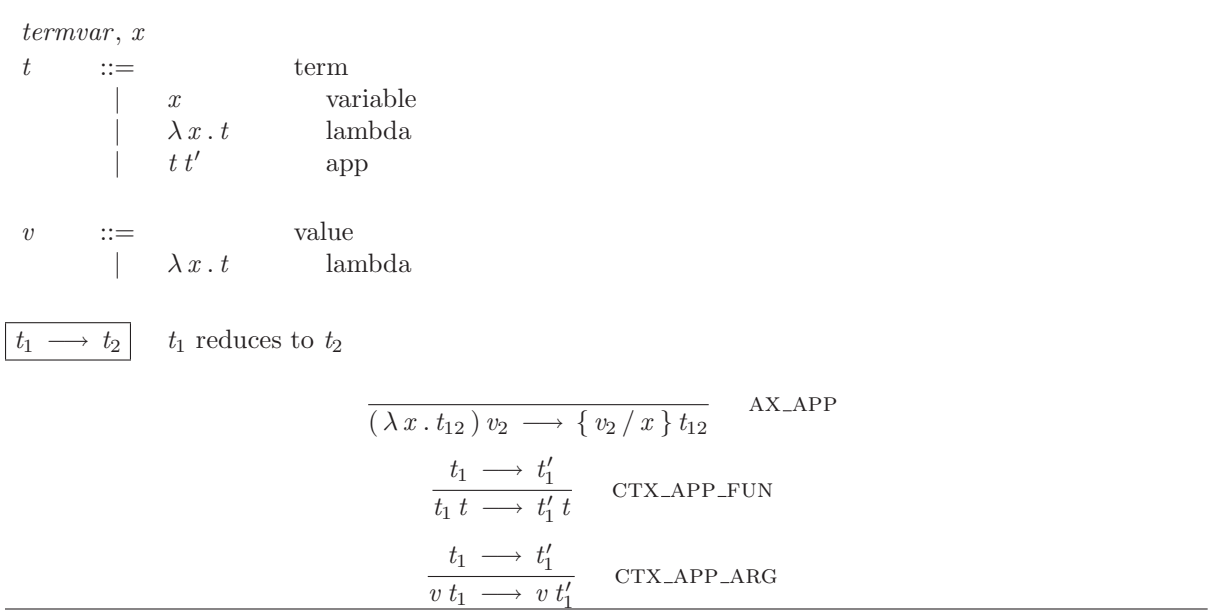

Figure 3: Generated LaTeX: `test10.2.tex`

```
metavar termvar, x ::=
  {{ tex \mathit{[[termvar]]} }}
```

Inside the `{{ tex ... }}` is some LaTeX code `\mathit{[[termvar]]}` giving the translation of a `termvar` or `x`. Here they are typeset in math italic (which in fact is also the default). Within the translation, the metavariable itself can be mentioned inside double square brackets `[[ ... ]]`.

Secondly, there is a grammar for a distinguished nonterminal root **terminals**, with a `{{ tex ... }}` translation for each, overriding the default typesetting of some terminals. Note that the other terminals (`. ( ) { } /`) are still given their default typesetting.

```
terminals :: 'terminals_' ::=
  | \            ::  :: lambda  {{ tex \lambda }}
  | -->          ::  :: red     {{ tex \longrightarrow }}
```

Thirdly, the file has **com** comments, including the `{{ com term }}` attached to a grammar rule, the `{{ com variable}}` attached to a production, and the `{{ com [[t1]] reduces to [[t2]]}}` attached to a semantic relation. These appear in the LaTeX output as shown in Figure 3.

4.1 Specifying LaTeX for productions

One can also specify **tex** translations for productions, overriding the default LaTeX typesetting, e.g. as in this example of a type abstraction production.

```
  |  X <: T . t   :: :: TLam   {{ tex \Lambda [[X]] [[<:]] [[T]]. \, [[t]] }}
```

These *homomorphisms*, or *homs*[1], can refer to the metavariables and nonterminals that occur in the production, e.g. the `[[X]]`, `[[T]]`, and `[[t]]` in the **tex** hom above, interleaved with arbitrary strings and with typeset elements of the **terminals** grammar, e.g. the `[[<:]]`.

Homomorphisms are applied recursively down the structure of symbolic terms. For example, an $F_{<:}$ term

```
(\X<:T11.t12) [T2]
```

would be LaTeX-pretty-printed, using the **tex** clause above, as

[1] Strictly, clauses of primitive recursive function definitions from symbolic terms to strings, here of LaTeX code.

```
( \, \Lambda  \mathit{X} <: \mathit{T_{\mathrm{11}}} . \, \mathit{t_{\mathrm{12}}} \, )
 \, \, [ \, \mathit{T_{\mathrm{2}}} \, ]
```

which is typeset as below.

$$(\Lambda X <: T_{11} . t_{12}) [T_2]$$

Note the `X`, `T11` and `t12` of the symbolic term are used to instantiate the formal parameters `X`, `T` and `t` of the homomorphism definition clause. If the `t` itself had compound term structure, e.g. as below

```
(\X<:T. \X'<:T'.x)
```

the homomorphism would be applied recursively, producing

```
( \, \Lambda  \mathit{X} <: \mathit{T} . \,  \Lambda  \mathit{X'} <: \mathit{T'}
. \,  \mathit{x} \,  \, )
```

typeset as follows.

$$(\Lambda X <: T . \Lambda X' <: T' . x)$$

Where there is no user-supplied homomorphism clause the LaTeX pretty-printing defaults to a sequence of the individual items separated by thin spaces (`\,`), with reasonable default fonts and making use of the `terminals` grammar where appropriate.

4.2 Specifying LaTeX for grammar rules

Grammar rules can include a **tex** hom specifying how all the nonterminal roots should be typeset, e.g.

```
type, t, s :: Typ_ ::=  {{ tex \mathsf{[[type]]} }}
      | unit                  ::   :: unit
      | type * type'          ::   :: pair
      | type -> type'         ::   :: fun
```

Alternatively, the individual nonterminal roots can have **tex** homs specifying how they should be typeset:

```
G {{ tex \Gamma }} , D {{ tex \Delta }} :: 'G_' ::=
      | empty                 ::   :: empty
      | G , x : T             ::   :: term
```

permitting the user to write `G'`, `D12` etc. in symbolic terms, to be typeset as Γ', Δ_{12}, etc.

4.3 Using the LaTeX code

The generated LaTeX code can be used in two main ways. By default, Ott generates a stand-alone LaTeX file, with a standard wrapper (including a `\documentclass`, various macro definitions, and a main body), that gives the complete system definition.

Alternatively, with the `-tex_wrap false` command-line argument, one can generate a file that can be included in other LaTeX files, that just defines macros to typeset various parts of the system.

The generated LaTeX output is factored into individual LaTeX commands: for the metavariable declarations, each rule of the syntax definition, the collected syntax (`\ottgrammar`), each rule of the inductive relation definitions, the collected rules for each relation, the collected rules for each `defns` block, the union of those (`\ottdefns`) and the whole (`\ottall`). This makes it possible to quote individual parts of the definition, possibly out-of-order, in a paper or technical report.

If one needs to include more than one system in a single LaTeX document, the `ott` prefix can be replaced using the `-tex_name_prefix` command-line argument.

The generated LaTeX is factored through some common style macros, e.g. to typeset a comment, a production, and a grammar. If necessary these can be redefined in an **embed** block (see Section 8.1). For example, the file `tests/squishtex.ott`

```
embed
 {{ tex
\renewcommand{\[[TEX_NAME_PREFIX]]grammartabular}[1]
  {\begin{minipage}{\columnwidth}\begin{tabular}{ll}#1\end{tabular}\end{minipage} }
\renewcommand{\[[TEX_NAME_PREFIX]]rulehead}[3]
  {$#1$  $#2$ & $#3$}
\renewcommand{\[[TEX_NAME_PREFIX]]prodline}[6]
  { \quad $#1$ \ $#2$ & \quad $#3 #4$  $#5$  $#6$}
\renewcommand{\[[TEX_NAME_PREFIX]]interrule}
  {\\[2.0mm]}
 }}
```

defines a more compact style for grammars. Note that the `[[TEX_NAME_PREFIX]]` is replaced by whatever prefix is in force, so such style files can be reused in different contexts.

A more sophisticated LaTeX package `ottlayout.sty`, providing fine control of how inference rules and grammars should be typeset, is contained in the `tex` directory of the distribution. It is described in the manual therein.

5 Generating proof assistant definitions

To generate proof assistant definitions, for Coq, Isabelle, and HOL, the minimal Ott source file of Section 3/Figure 1 must be extended with a modest amount of additional data, as shown in Figure 4. Executing

```
bin/ott -coq out.v  -isabelle out.thy  -hol outScript.sml  tests/test10.4.ott
```

generates Coq `out.v`, Isabelle `out.thy`, and HOL `outScript.sml`, shown in Figures 5, 6, and 7. The additional data can be combined with the annotations for LaTeX of the previous section, but those are omitted here. We add four things. First, we specify proof assistant types to represent object-language variables — in this example, choosing the `string` type of Isabelle and HOL, and the `nat` type for Coq:

```
metavar termvar, x ::=
{{ isa string}} {{ coq nat}} {{ hol string}} {{ coq-equality }}
```

For Coq output, one can specify `{{ coq-equality` *proof-script* `}}` to build a decidable equality over the Coq representation type using the proof *proof-script*. If the script is omitted, as in this example, it defaults to

```
Proof.
  decide equality; auto with ott_coq_equality arith.
Defined.
```

where the `ott_coq_equality` database contains the decidable equalities of the representation types defined in the source. It is possible to turn off type generation for metavariables, by adding the declaration `{{ phantom }}`. This is useful in some cases, for instance to avoid duplicate definitions of types already defined in an imported library.

Second, we specify what the binding is in the object language, with the `(+ bind x in t +)` annotation on the `Lam` production:

```
| \ x . t      ::  :: Lam     (+ bind x in t +)
```

Section 9 describes the full language of binding specifications.

Third, we add a block

```
substitutions
  single t x :: tsubst
```

to cause Ott to generate Coq/Isabelle/HOL definitions of a substitution function, with name root `tsubst`, replacing metavariables `x` by terms `t`. This is for single substitutions; multiple substitution functions

```
% minimal                      + binding + subst + coq/hol/isa
metavar termvar, x ::=
{{ isa string}} {{ coq nat}} {{ hol string}} {{ coq-equality }}

grammar
t :: 't_' ::=
  | x             ::  :: Var
  | \ x . t       ::  :: Lam      (+ bind x in t +)
  | t t'          ::  :: App
  | ( t )         :: S:: Paren    {{ icho [[t]]  }}
  | { t / x } t'  :: M:: Tsub     {{ icho (tsubst_t [[t]] [[x]] [[t']])}}

v :: 'v_' ::=
  | \ x . t       ::  :: Lam

subrules
  v <:: t

substitutions
  single t x :: tsubst

defns
Jop :: '' ::=

 defn
 t1 --> t2 :: ::reduce::''  by


    ---------------------------  :: ax_app
    (\x.t12) v2 -->  {v2/x}t12

    t1 --> t1'
    -------------- :: ctx_app_fun
    t1 t --> t1' t

    t1 --> t1'
    -------------- :: ctx_app_arg
    v t1 --> v t1'
```

Figure 4: Source: `test10.4.ott`

(taking lists of substitutand/substitutee pairs) can also be generated with the keyword **multiple**. Substitution functions are generated for all rules of the grammar for which they might be required — here, just over `t`, with a function named `tsubst_t`.

Finally, we specify translations for the metaproductions:

```
  | ( t )          :: S:: Paren   {{ icho [[t]]  }}
  | { t / x } t'  :: M:: Tsub    {{ icho (tsubst_t [[t]] [[x]] [[t']])}}
```

These specify that `(t)` should be translated into just the translation of `t`, whereas `{t/x}t'` should be translated into the proof-assistant application of `tsubst_t` to the translations of `t`, `x`, and `t'`. The (admittedly terse) **icho** specifies that these translations should be done uniformly for Isabelle, Coq, HOL, and OCaml output. One can also specify just one of these, writing {{ **coq** ...}}, {{ **hol** ...}}, {{ **isa** ...}}, or {{ **ocaml** ...}}, or include several, with different translations for each. There are also abbreviated forms **ich**, **ic**, **ch**, and **ih**. The body of a proof assistant hom should normally include outer parentheses, as in the `Tsub` hom above, so that it is parsed correctly by the proof assistant in all contexts.

5.1 Proof assistant code for grammar rules

The normal behaviour is to generate a free proof assistant type for each (non-subrule) grammar rule. For example, the Coq compilation for `t` here generates a free type with three constructors:

```
Inductive
t : Set :=
   t_Var : termvar -> t
 | t_Lam : termvar -> t -> t
 | t_App : t -> t -> t .
```

(note that the metaproductions do not give rise to constructors).

One can instead specify an arbitrary proof assistant representation type, annotating the grammar rule with a **coq**, **isa**, **hol**, or **ocaml** hom — for example, in the following grammar for substitutions.

```
s {{ tex \sigma }} :: 'S_' ::= {{ com multiple subst }} {{ isa (termvar*t) list }}
     | [ x |-> t ]            ::   :: singleton   {{ isa [ ([[x]],[[t]]) ]  }}
     | s1 , .. , sn           ::   :: list        {{ isa List.concat [[s1 .. sn]] }}
```

Here the {{ **isa** `(termvar*t) list` }} hom specifies that in Isabelle output this type be represented as an Isabelle `(termvar*t) list` instead of the default free inductive type; all the productions are metaproductions (tagged **M**); and **isa** homs for each production specify how they should be translated into that Isabelle type. This feature must be used with care, as any Ott-generated functions, e.g. substitution functions, cannot recurse through such user-defined types.

Grammar rules (whether free or non-free) can also include a **coq equality** hom, instructing the Coq code generator to derive a decidable equality for the Coq representation type. For example, the ML polymorphism Ott source of `test8.ott` includes the following.

```
typvar :: TV_ ::= {{ coq-equality decide equality. apply eq_value_name_t. }}
     | ' ident                ::   :: ident
```

The Coq/HOL/Isabelle/OCaml type name for a grammar rule, or for a metavariable declaration, is normally taken to be just its primary nonterminal root. Occasionally it is useful to work around a clash between a metavar or nonterminal primary root and a proof assistant symbol, e.g. `T` in HOL or `value` in Isabelle. For this, one can add a **coq**, **hol**, **isa**, or **ocaml** hom to the primary nonterminal root. In the example below, the user can write `T`, `T'` etc. in their Ott source, but the generated HOL type is `Typ`.

```
T {{ hol Typ }}, S, U :: 'T_' ::=                  {{ com type  }}
  | T -> T'                          :: :: Fun        {{ com type of functions }}
```

The grammar rules of a syntax definition may depend on each other arbitrarily. When generating Isabelle/Coq/HOL/OCaml representation types, however, they are topologically sorted, to simplify the resulting induction principles.

```
(* generated by Ott 0.10.16 from: ../tests/non_super_tabular.ott ../tests/test10.ott *)

Require Import Arith.
Require Import Bool.
Require Import List.

(** syntax *)
Definition termvar := nat.
Lemma eq_termvar: forall (x y : termvar), {x = y} + {x <> y}.
Proof.
  decide equality; auto with ott_coq_equality arith.
Defined.
Hint Resolve eq_termvar : ott_coq_equality.


Inductive t : Set :=
 | t_Var : termvar -> t
 | t_Lam : termvar -> t -> t
 | t_App : t -> t -> t.


(** library functions *)
Fixpoint list_mem (A:Set) (eq:forall a b:A,{a=b}+{a<>b}) (x:A) (l:list A) {struct l} : bool :=
  match l with
  | nil => false
  | cons h t => if eq h x then true else list_mem A eq x t
end.
Implicit Arguments list_mem.


(** subrules *)
Definition is_v_of_t (t_6:t) : Prop :=
  match t_6 with
  | (t_Var x) => False
  | (t_Lam x t5) => (True)
  | (t_App t5 t') => False
end.


(** substitutions *)
Fixpoint tsubst_t (t_6:t) (x5:termvar) (t__7:t) {struct t__7} : t :=
  match t__7 with
  | (t_Var x) => (if eq_termvar x x5 then t_6 else (t_Var x))
  | (t_Lam x t5) => t_Lam x (if list_mem eq_termvar x5 (cons x nil) then t5 else (tsubst_t t_6 x5 t5))
  | (t_App t5 t') => t_App (tsubst_t t_6 x5 t5) (tsubst_t t_6 x5 t')
end.


(** definitions *)

(* defns Jop *)
Inductive reduce : t -> t -> Prop :=    (* defn reduce *)
 | ax_app : forall (x:termvar) (t12 v2:t),
     is_v_of_t v2 ->
     reduce (t_App  (t_Lam x t12)  v2)  (tsubst_t  v2   x   t12 )
 | ctx_app_fun : forall (t1 t_5 t1':t),
     reduce t1 t1' ->
     reduce (t_App t1 t_5) (t_App t1' t_5)
 | ctx_app_arg : forall (v5 t1 t1':t),
     is_v_of_t v5 ->
     reduce t1 t1' ->
     reduce (t_App v5 t1) (t_App v5 t1').
```

Figure 5: Generated Coq:`test10.v`

```
(* generated by Ott 0.10.16 from: ../tests/non_super_tabular.ott ../tests/test10.ott *)
theory test10
imports Main Multiset
begin

(** syntax *)
types termvar = "string"

datatype t =
   t_Var "termvar"
 | t_Lam "termvar" "t"
 | t_App "t" "t"



(** subrules *)
consts
is_v_of_t :: "t => bool"
primrec
"is_v_of_t (t_Var x) = (False)"
"is_v_of_t (t_Lam x t) = ((True))"
"is_v_of_t (t_App t t') = (False)"


(** substitutions *)
consts
tsubst_t :: "t => termvar => t => t"
primrec
"tsubst_t t5 x5 (t_Var x) = ((if x=x5 then t5 else (t_Var x)))"
"tsubst_t t5 x5 (t_Lam x t) = (t_Lam x (if x5 mem [x] then t else (tsubst_t t5 x5 t)))"
"tsubst_t t5 x5 (t_App t t') = (t_App (tsubst_t t5 x5 t) (tsubst_t t5 x5 t'))"


(** definitions *)
(*defns Jop *)
inductive reduce :: "t \<Rightarrow> t \<Rightarrow> bool"
where
(* defn reduce *)

ax_appI: "\<lbrakk>is_v_of_t v2\<rbrakk> \<Longrightarrow>
reduce ((t_App  (t_Lam x t12)  v2)) ( (tsubst_t  v2   x   t12 ) )"

| ctx_app_funI: "\<lbrakk>reduce (t1) (t1')\<rbrakk> \<Longrightarrow>
reduce ((t_App t1 t)) ((t_App t1' t))"

| ctx_app_argI: "\<lbrakk>is_v_of_t v ;
reduce (t1) (t1')\<rbrakk> \<Longrightarrow>
reduce ((t_App v t1)) ((t_App v t1'))"



end
```

Figure 6: Generated Isabelle:`test10.thy`

```
(* generated by Ott 0.10.16 from: ../tests/non_super_tabular.ott ../tests/test10.ott *)
(* to compile: Holmake test10Theory.uo   *)
(* for interactive use:
  app load ["pred_setTheory","finite_mapTheory","stringTheory","containerTheory","ottLib"];
*)

open HolKernel boolLib Parse bossLib ottLib;
infix THEN THENC |-> ## ;
local open arithmeticTheory stringTheory containerTheory pred_setTheory listTheory
  finite_mapTheory in end;

val _ = new_theory "test10";

(** syntax *)
val _ = type_abbrev("termvar", ``:string``);
val _ = Hol_datatype `
t =
   t_Var of termvar
 | t_Lam of termvar => t
 | t_App of t => t
`;


(** subrules *)
val _ = ottDefine "is_v_of_t" `
    ( is_v_of_t (t_Var x) = F)
/\  ( is_v_of_t (t_Lam x t) = (T))
/\  ( is_v_of_t (t_App t t') = F)
`;

(** substitutions *)
val _ = ottDefine "tsubst_t" `
    ( tsubst_t t5 x5 (t_Var x) = (if x=x5 then t5 else (t_Var x)))
/\  ( tsubst_t t5 x5 (t_Lam x t) = t_Lam x (if MEM x5 [x] then t else (tsubst_t t5 x5 t)))
/\  ( tsubst_t t5 x5 (t_App t t') = t_App (tsubst_t t5 x5 t) (tsubst_t t5 x5 t'))
`;

(** definitions *)
(* defns Jop *)

val (Jop_rules, Jop_ind, Jop_cases) = Hol_reln `
(* defn reduce *)

( (* ax_app *)  !(x:termvar) (t12:t) (v2:t) . (clause_name "ax_app") /\
((is_v_of_t v2))
 ==>
( ( reduce (t_App  (t_Lam x t12)  v2)  (tsubst_t  v2   x   t12 )  )))

/\ ( (* ctx_app_fun *)  !(t1:t) (t:t) (t1':t) . (clause_name "ctx_app_fun") /\
(( ( reduce t1 t1' )))
 ==>
( ( reduce (t_App t1 t) (t_App t1' t) )))

/\ ( (* ctx_app_arg *)  !(v:t) (t1:t) (t1':t) . (clause_name "ctx_app_arg") /\
((is_v_of_t v) /\
( ( reduce t1 t1' )))
 ==>
( ( reduce (t_App v t1) (t_App v t1') )))

`;



val _ = export_theory ();
```

Figure 7: Generated HOL:`test10Script.sml`

5.2 Proof assistant code for inductive definitions

The semantic relations are defined with the proof-assistant inductive relations packages, `Inductive`, `Hol_reln`, and `inductive_set` or `inductive`, respectively. Each **`defns`** block gives rise to a potentially mutually recursive definition of each **`defn`** inside it (it seems clearer not to do a topological sort here). Definition rules are expressed internally with symbolic terms. We give a simplified grammar thereof in Fig. 17, omitting the symbolic terms for list forms. A symbolic term *st* for a nonterminal root is either an explicit nonterminal or a node, the latter labelled with a production name and containing a list of *symterm_elements*, which in turn are either symbolic terms, metavariables, or variables. Each definition rule gives rise to an implicational clause, essentially that the premises (Ott symbolic terms of the **`formula`** grammar) imply the conclusion (an Ott symbolic term of whichever judgement is being defined). Symbolic terms are compiled in several different ways:

- Nodes of non-meta productions are output as applications of the appropriate proof-assistant constructor (and, for a subrule, promoted to the corresponding constructor of a maximal rule).
- Nodes of meta productions are transformed with the user-specified homomorphism.
- Nodes of judgement forms are represented as applications of the defined relation in Coq and HOL, and as set-membership assertions in Isabelle.
- Lists of formulae (the `formula_dots` production, c.f.§11) are special-cased to proof-assistant conjunctions.

Further, for each nonterminal of a non-free grammar rule, e.g. a usage of `v'` where `v<::t`, an additional premise invoking the generated subrule predicate for the non-free rule is added, e.g. `is_v v'`. For Coq and HOL, explicit quantifiers are introduced for all variables mentioned in the rule. For HOL, rules are tagged with their rule name (using `clause_name`).

5.3 Representation of binding

At present the generated Isabelle/Coq/HOL uses fully concrete representations of variables in terms, without any notion of alpha equivalence, as one can see in Fig. 6: see the `t` datatype of terms and the `tsubst_t` substitution function there. An experimental Coq backend generates definitions in locally-nameless style for a subset of the Ott metalanguage. This is work-in-progress, and it is extensively documented in `http://moscova.inria.fr/ zappa/projects/ln_ott/`. We intend in future to generate other representations, and in some circumstances homs can be used to implement other representations directly. For a reasonably wide variety of languages, however, one can capture the intended semantics of whole programs in this idiom, subject only to the condition that standard library identifiers are not shadowed within the program, as the operational semantics does not involve reduction under binders — so any substitutions are of terms which (except for standard library identifiers) are closed. This includes the ML polymorphism example of `test8.ott`. For languages which require a type environment with internal dependencies, however, for example $F_{<:}$, this is no longer the case. The POPLmark $F_{<:}$ example given in `test7.ott` has a type system which disallows all shadowing, a property that is not preserved by reduction. However, a correct translation of $F_{<:}$ is generated by the Coq locally-nameless backend, and can be found in `http://moscova.inria.fr/ zappa/projects/ln_ott/`.

Further discussion of binding representations is in the Ott ICFP 2007 paper and in a working draft

> Binding and Substitition. Susmit Sarkar, Peter Sewell, and Francesco Zappa Nardelli. August 2007.

available from the Ott web page.

5.4 Correctness of the generated proof assistant code

We have attempted to ensure that the proof assistant definitions generated by Ott are well-formed and what the user would intend. This is not guaranteed, however, for several reasons: (1) There may be name clashes between Ott-generated identifiers and proof assistant built-in identifiers (or, in pathological

cases, even among different Ott-generated identifiers). (2) In some cases we depend on automatic proof procedures, e.g. for HOL definitions. These work in our test cases, but it is hard to ensure that they will in all cases. More importantly, (3) the generation process is complex, so it is quite possible that there is either a bug in Ott or a mismatch between the user expectation and what the tool actually does. Ultimately one has to read the generated proof assistant definitions to check that they are as intended — but typically one would do this in any case, many times over, in the process of proving metatheoretic results, so we do not consider it a major issue.

5.5 Using the generated proof assistant code

Ott builds code for

Coq 8.1	`http://coq.inria.fr/`
HOL 4 (the current svn version)	`http://hol.sourceforge.net/`
Isabelle/HOL (Isabelle 2008)	`http://isabelle.in.tum.de/`

Given proof assistant files in the top-level directory of the distribution, as produced at the start of this section (Coq `out.v`, Isabelle `out.thy`, and HOL `outScript.sml`), the various proof assistants can be invoked as follows.

5.5.1 Coq

First run

```
make
```

in the `coq` directory of the distribution, to build the auxiliary files. These include a core file (`ott_list_core`) of definitions that are used in Ott-generated output. At present these are only required when Coq native lists are used. There are also various lemmas (in `ott_list.v`) which may be useful; they can be made available with `Require Import ott_list.`

For batch mode run

```
coqc -I coq  out.v
```

where `coq` is the path to the `coq` directory of the distribution.

The experimental locally-nameless backend requires the `Metatheory` library by Arthur Charguéraud, available from the project web page.

5.5.2 HOL

First run

```
Holmake
```

in the `hol` directory of the distribution, to build the auxiliary files.

For batch mode run

```
Holmake -I hol  outTheory.uo
```

where `hol` is the path to the `hol` directory of the distribution. For interactive mode, run

```
hol -I hol
```

inside an editor window (where the second `hol` is again the path to the `hol` directory of the distribution), and in another window view the `outScript.sml` file. First paste in the `app load` command from a comment at the top of the file, then paste in the remainder.

5.5.3 Isabelle

For batch mode:

```
echo 'use_thy "out" ;' | isabelle
```

or (to give an appropriate exit status if there is a failure):

```
echo 'use_thy "out" handle e => (OS.Process.exit OS.Process.failure);' | isabelle
```

Interactively, using Proof General:

```
Isabelle out.thy
```

6 Judgments and formulae

In a semantic rule, for example

```
t1 --> t1'
-------------- :: ctx_app_arg
v t1 --> v t1'
```

the conclusion must be a symbolic term of the form of the judgement being defined, but in general the premises may be symbolic terms of a **formula** grammar. By default this includes all the defined judgement forms: for the running example Ott will synthesise grammars as below.

formula	::=		
	|	*judgement*	
judgement	::=		
	|	*Jop*	
Jop	::=		
	|	$t_1 \longrightarrow t_2$	t_1 reduces to t_2

The user can also define an explicit formula grammar, to let other forms (not just judgements) appear as rule premises. Below is a fragment of the formula grammar from the LJ example on the Ott web page.

```
formula :: formula_ ::=
  |  judgement                          ::   :: judgement
  |  formula1 .. formulan               ::   :: dots
  |  not formula                        :: M :: not
         {{ tex \neg [[formula]] }}
         {{ isa \<not> ([[formula]]) }}
  |  ( formula )                       :: M :: brackets
         {{ tex ([[formula]]\!) }}
         {{ isa [[formula]] }}
  |  formula \/ formula'               :: M :: or
         {{ tex [[formula]] \vee [[formula']] }}
         {{ isa [[formula]] \<or> [[formula']] }}
  |  formula /\ formula'               :: M :: and
         {{ tex [[formula]] \wedge [[formula']] }}
         {{ isa [[formula]] \<and> [[formula']] }}
  |  x = x'                            :: M :: xali
         {{ isa [[x]] = [[x']] }}
  |  X = X'                            :: M :: Xali
         {{ isa [[X]] = [[X']] }}
```

This example adds (to the judgement forms) syntax for parenthesised formulae, negation, and, or, and equality testing on two sorts. For each, **tex** and **isa** homs specify how they should be typeset and be translated into Isabelle.

If the user defines a **formula** grammar then (as here) the production name prefix must be `formula_` and the name for the `judgement` production must be `judgement`.

The tool also synthesises a `user_syntax` grammar of all the user syntax, for example:

user_syntax ::=
| *termvar*
| *t*
| *v*
| *terminals*

7 Concrete terms and OCaml generation

In semantic definitions, one typically never uses concrete variables, only metavariables that range over them. In examples, however, one may need either a mix of concrete variables and metavariables, or, for strictly concrete terms, to restrict to just the former (and also to prohibit symbolic nonterminals).

Figure 2 combines the LaTeX and proof assistant annotations of Sections 3 and 4, adding a {{ **lex** `alphanum`}} hom to the **metavar** declaration to specify the lexical form of concrete variables of this sort. At present a **lex** homomorphism must have body either **Alphanum** (standing for `[A-Z]([A-Z]|[a-z]|[0-9]|'|_)*`), **alphanum** (for `([A-Z]|[a-z])([A-Z]|[a-z]|[0-9]|'|_)*`), **alphanum0** (for `[a-z]([A-Z]|[a-z]|[0-9]|'|_)*`), or **numeral** (for `[0-9][0-9]*`); more general regular expressions are not supported. An identifier that can be ambiguously lexed as either a concrete or symbolic metavariable, e.g. `x` in the scope of the above declaration, will be taken to be symbolic. To restrict the parser to strictly concrete terms only, one can add a **:concrete:** prefix, as shown in Figure 10.

One can also specify how concrete variables should be LaTeX'd or translated into a proof assistant, e.g. with homomorphisms {{ **texvar** `\mathrm{[[termvar]]}`}} and {{ **isavar** `''[[termvar]]''`}} (and similarly **coqvar**, **holvar**, and **ocamlvar**).

Figure 2 also specifies an OCaml representation type for variables, with the **metavar** hom {{ **ocaml** `int`}}. Executing

```
bin/ott -ocaml test10.ml  tests/test10.ott
```

produces the OCaml code shown in Figure 9, including OCaml types to represent the abstract syntax, and auxiliary functions for subrules and substitutions. This does not implement the semantic rules. In some cases the various proof assistant code extraction facilities can be used — see Section 18.

8 Filtering: Using Ott syntax within LaTeX, Coq, Isabelle, HOL, or OCaml

8.1 Filtering embedded code

It is possible to embed arbitrary code in the Ott source using an `embed` block, which can contain **tex**, **coq**, **hol**, **isa**, or **ocaml** homomorphisms, the bodies of which will appear in the respective output. Depending on the position of the `embed` section, this will either be at the beginning of the output file, between the generated functions (substitution etc.) and the definitions of inductive relations, or at the end of the file (for any after the first definition, the `embed` keyword must be on a line by itself). For example, `test8.ott` contains the following to define Coq and HOL `remove_duplicates` functions.

```
embed
{{ coq
Fixpoint remove_duplicates (l:list typvar_t) : list typvar_t :=
  match l with
  | nil => nil
  | cons h t => if (list_mem eq_typvar_t h t)  then remove_duplicates t
                else cons h (remove_duplicates t)
```

```
% all
metavar termvar, x ::=   {{ com  term variable }}
{{ isa string}} {{ coq nat}} {{ hol string}} {{ coq-equality }}
{{ ocaml int}} {{ lex alphanum}} {{ tex \mathit{[[termvar]]} }}

grammar
t :: 't_' ::=                                {{ com term    }}
  | x            ::  :: Var                    {{ com variable}}
  | \ x . t      ::  :: Lam (+ bind x in t +) {{ com lambda  }}
  | t t'         ::  :: App                    {{ com app     }}
  | ( t )        :: S:: Paren                  {{ icho [[t]]  }}
  | { t / x } t' :: M:: Tsub
                       {{ icho (tsubst_t [[t]] [[x]] [[t']])}}

v :: 'v_' ::=                                {{ com value   }}
  | \ x . t      ::  :: Lam                    {{ com lambda  }}

terminals :: 'terminals_' ::=
  | \            ::  :: lambda  {{ tex \lambda }}
  | -->          ::  :: red     {{ tex \longrightarrow }}

subrules
  v <:: t

substitutions
  single t x :: tsubst

defns
Jop :: '' ::=

 defn
 t1 --> t2 :: ::reduce::'' {{ com [[t1]] reduces to [[t2]]}} by


    -------------------------  :: ax_app
    (\x.t12) v2 -->  {v2/x}t12

    t1 --> t1'
    -------------- :: ctx_app_fun
    t1 t --> t1' t

    t1 --> t1'
    -------------- :: ctx_app_arg
    v t1 --> v t1'
```

Figure 8: Source: `test10.7.ott`

```
(* generated by Ott 0.10.16 from: ../tests/non_super_tabular.ott ../tests/test10.ott *)

(** syntax *)
type termvar = int

type
t =
   T_Var of termvar
 | T_Lam of termvar * t
 | T_App of t * t



(** subrules *)
let is_v_of_t (t5:t) : bool =
  match t5 with
  | (T_Var x) -> false
  | (T_Lam (x,t)) -> (true)
  | (T_App (t,t')) -> false



(** substitutions *)
let rec tsubst_t (t5:t) (x5:termvar) (t_6:t) : t =
  match t_6 with
  | (T_Var x) -> (if x=x5 then t5 else (T_Var x))
  | (T_Lam (x,t)) -> T_Lam (x,(if List.mem x5 [x] then t else (tsubst_t t5 x5 t)))
  | (T_App (t,t')) -> T_App ((tsubst_t t5 x5 t),(tsubst_t t5 x5 t'))



(* defns not defined in OCaml output *)
```

Figure 9: Generated OCaml code: `test10.ml`

```
end. }}

{{ hol
val _ = Define `
  (remove_duplicates [] = []) /\
  (remove_duplicates (x::xs) = if (MEM x xs) then remove_duplicates xs
                               else x::(remove_duplicates xs))
`; }}
```

Within the body of an **embed** homomorphism, any text between `[[` and `]]` will be parsed as a symbolic term (of the `user_syntax` grammar) and pretty printed, so one can use user syntax within LaTeX or proof assistant code. An Isabelle example is below, defining an Isabelle function to calculate the order of a type with productions `unit`, `t*t'`, and `t->t'`.

```
{{ isa
consts
order :: "type => nat"
primrec
"order [[unit]] = 0"
"order [[t*t']] = max (order [[t]]) (order [[t']])"
"order [[t->t']] = max (1+order [[t]]) (order [[t']])"

}}
```

It is often useful to define a proof assistant function, in an **embed** section, together with a production of the **formula** grammar with a proof assistant hom that uses that function, thereby introducing syntax that lets the function be used in semantic rules.

8.2 Filtering files

Similar processing can be carried out on separate files, using the command-line options `tex_filter`, `isa_filter`, etc. Each of these takes two arguments, a source filename and a destination filename. In processing the source file, any text between `[[` and `]]` will be parsed as a symbolic term (of the `user_syntax` grammar) and pretty printed in the appropriate style. All other text is simply echoed.

Typical usage for LaTeX would be something like this (from the `Makefile` used to produce this document):

```
test7.tex: ../src/ott ../tests/test7.ott ../tests/test7tt.mng
         cd ../src; make tmp_test7_clean.ott
         ../src/ott                                          \
                -tex test7.tex                               \
                -tex_show_meta false                         \
                -tex_wrap false                              \
                -tex_name_prefix testSeven                   \
                -tex_filter ../tests/test7tt.mng test7tt.tex \
                ../src/tmp_test7_clean.ott
```

The `-tex_wrap false` turns off output of the default LaTeX document preamble, so the generated file `test7.tex` just contains LaTeX definitions. The `-tex_name_prefix testSeven` sets a prefix for the generated LaTeX commands (so the LaTeX definitions from multiple Ott source files can be included in a single LaTeX document). The `-tex_filter` argument takes two filenames, a source and a destination. It filters the source file, (roughly) replacing any string found within `[[ ]]` by the tex pretty-print of its parse. This parsing is done w.r.t. the generated nonterminal `user_syntax` which is a union of all the user's grammar.

At present munged strings are not automatically put within `$ $`, and there is no analogue of the `<[ ]>` of our previous munger.

The lexing turns any sequence of `[` (resp. of `]`) of length $n+1$ for $n > 2$ into a literal sequence of length n.

```
We can TeX-typeset symbolic terms of the language, e.g.
\[ [[ (\X<:Top. \x:X.x) [Top->Top] ]]\]
and concrete terms
\[ [[ :concrete: \Z1<:Top. \x:Z1.x ]]\]
and similarly judgements etc, e.g.
\[ [[G |- t : T ]] \]

Here is an extract of the syntax:

\testSevengrammartabular{\testSevent\testSevenafterlastrule}

and a single semantic rule:

\[\testSevendruletinXXTwo{}\]

and a judgement definition:

\testSevendefnSA

One can also include a ‘defns’ collection of judgements, or the complete definition.
% \section{Full Definition}
% \testSevenmetavars\\[0pt]
% \testSevengrammar\\[0pt]
% \testSevendefnss
%
% \testSevenall
```

Figure 10: $F_{<:}$ Extracts: LaTeX source file to be filtered (`test7tt.mng`)

Figures 10 and 11 show a source file (`test7tt.mng`) that uses terms of the $F_{<:}$ definition of `test7.ott`, and the result of filtering it.

Similar filtering can be performed on Coq, Isabelle, HOL, and OCaml files.

To filter files with respect to a relatively stable system definition, without having to re-process the Ott source files of that system definition each time, there are command-line options

```
-writesys <filename>                Output system definition
-readsys <filename>                 Input system definition
```

to first write the system definition (generated from some source files) to a file, and then to read one back in (instead of re-reading the Ott source files). The saved system definitions are in an internal format, produced using the OCaml marshaller, and contain OCaml closures. They therefore will not be compatible between different Ott versions. They may also be quite large.

9 Binding specifications

Our first example involved a production with a single binder:

$$\begin{array}{lll} t & ::= & \\ & \mid & \lambda\, x\, .\, t \quad \mathsf{bind}\ x\ \mathsf{in}\ t \qquad \mathrm{Lam} \end{array}$$

specified by the source shown in Figure 4:

```
  | \ x . t      ::  :: Lam     (+ bind x in t +)
```

We can TeX-typeset symbolic terms of the language, e.g.

$$(\,\Lambda X{<:}\mathbf{Top}.\,\lambda x{:}X.\,x\,)\,[\,\mathbf{Top}\,\rightarrow\,\mathbf{Top}\,]$$

and concrete terms

$$\Lambda \mathrm{Z1}{<:}\mathbf{Top}.\,\lambda \mathrm{x}{:}\mathrm{Z1}.\,\mathrm{x}$$

and similarly judgements etc, e.g.

$$\Gamma \vdash t : T$$

Here is an extract of the syntax:

t	::=			term
	|	x		variable
	|	$\lambda x{:}T.\,t$	bind x in t	abstraction
	|	$t\,t'$		application
	|	$\Lambda X{<:}T.\,t$	bind X in t	type abstraction
	|	$t\,[\,T\,]$		type application
	|	$\{\,l_1{=}t_1\,,\,..\,,\,l_n{=}t_n\,\}$		record
	|	$t\,.\,l$		projection
	|	$\mathbf{let}\,p{=}t\,\mathbf{in}\,t'$	bind $\mathrm{b}(p)$ in t'	pattern binding

and a single semantic rule:

$$\frac{x : T \in \Gamma}{x : T \in \Gamma\,,\,X' <:\,U'}\quad \textsc{tin\_2}$$

and a judgement definition:

$\boxed{\Gamma \vdash S <:\,T}$ S is a subtype of T

$$\frac{\Gamma \vdash \mathbf{ok}}{\Gamma \vdash S <:\,\mathbf{Top}}\quad \textsc{SA\_Top}$$

$$\frac{\Gamma \vdash \mathbf{ok}}{\Gamma \vdash X <:\,X}\quad \textsc{SA\_Refl\_TVar}$$

$$\frac{X <:\,U \in \Gamma \qquad \Gamma \vdash U <:\,T}{\Gamma \vdash X <:\,T}\quad \textsc{SA\_Trans\_TVar}$$

$$\frac{\Gamma \vdash T_1 <:\,S_1 \qquad \Gamma \vdash S_2 <:\,T_2}{\Gamma \vdash S_1 \rightarrow S_2 <:\,T_1 \rightarrow T_2}\quad \textsc{SA\_Arrow}$$

$$\frac{\Gamma \vdash T_1 <:\,S_1 \qquad \Gamma\,,\,X <:\,T_1 \vdash S_2 <:\,T_2}{\Gamma \vdash \forall X{<:}S_1.\,S_2 <:\,\forall X{<:}T_1.\,T_2}\quad \textsc{SA\_All}$$

$$\frac{\forall i \in 1..m.\exists j \in 1..n.(\,k_i{=}l_j \,\wedge\, \Gamma \vdash S_i <:\,T_j\,)}{\Gamma \vdash \{\,k_1 : S_1\,,\,..\,,\,k_m : S_m\,\} <:\,\{\,l_1 : T_1\,,\,..\,,\,l_n : T_n\,\}}\quad \textsc{SA\_Rcd}$$

One can also include a 'defns' collection of judgements, or the complete definition.

Figure 11: $\mathrm{F}_{<:}$ Extracts: the filtered output (`test7tt.tex`)

in which a single variable binds in a single subterm. Realistic programming languages often have much more complex binding structures, e.g. structured patterns, multiple mutually recursive `let` definitions, comprehensions, or-patterns, and dependent record patterns.

Ott has a flexible metalanguage for specifying binding structures, expressive enough to cover these. It comprises two forms of annotation on productions. The first, $\mathsf{bind}\ mse\ \mathsf{in}\ nonterm$, lets one specify that variables bind in nonterminals of the production, as in the `Lam` production above. Here mse is a *metavariable set expression*, e.g. in that lambda production just the singleton metavariable x of the production. A variable can bind in multiple nonterminals, as in the example of a simple recursive `let` below.

$$
\begin{array}{lll}
t ::= & & \\
\quad \mid \ \mathbf{let\,rec}\ x\ =\ t\ \mathbf{in}\ t' & & \mathsf{bind}\ x\ \mathsf{in}\ t \\
 & & \mathsf{bind}\ x\ \mathsf{in}\ t'
\end{array}
$$

More complex examples require one to collect together sets of variables. For example, the grammar below (shown in Ott source and the generated LaTeX) has structured patterns, with a $\mathbf{let}\ p\ =\ t\ \mathbf{in}\ t'$ production in which all the binders of the pattern p bind in the continuation t'.

```
t :: E_ ::=
  | x                          ::   :: ident
  | ( t1 , t2 )                ::   :: pair
  | let p = t in t'            ::   :: letrec      (+ bind binders(p) in t' +)


p :: P_ ::=
  | _                          ::   :: wildcard    (+ binders = {} +)
  | x                          ::   :: ident       (+ binders = x +)
  | ( p1 , p2 )                ::   :: pair        (+ binders = binders(p1) union binders(p2) +)
```

$$
\begin{array}{lll}
t ::= & & \\
\quad \mid \ x & & \\
\quad \mid \ (\, t_1\ ,\ t_2\,) & & \\
\quad \mid \ \mathbf{let}\ p\ =\ t\ \mathbf{in}\ t' & & \mathsf{bind}\ \mathrm{binders}(p)\ \mathsf{in}\ t' \\
p ::= & & \\
\quad \mid \ \_ & & \mathrm{binders} = \{\} \\
\quad \mid \ x & & \mathrm{binders} = x \\
\quad \mid \ (\, p_1\ ,\ p_2\,) & & \mathrm{binders} = \mathrm{binders}(p_1) \cup \mathrm{binders}(p_2)
\end{array}
$$

This is expressed with the second form of annotation: user-defined *auxiliary functions* such as the binders above. This is an auxiliary function defined over the p grammar that identifies a set of variables to be used in the bind annotation on the **let** production. There can be any number of such auxiliary functions; binders is not a distinguished keyword.

The syntax of a precise fragment of the binding metalanguage is given in Fig. 12, where we have used Ott to define part of the Ott metalanguage. A simple type system (not shown) enforces sanity properties, e.g. that each auxiliary function is only applied to nonterminals that it is defined over, and that metavariable set expressions are well-sorted.

Further to that fragment, the tool supports binding for the list forms of §11. Metavariable set expressions can include lists of metavariables and auxiliary functions applied to lists of nonterminals, e.g. as in the record patterns below.

$$
\begin{array}{lll}
p ::= & & \\
\quad \mid \ x & & \mathrm{b} = x \\
\quad \mid \ \{\, l_1\ =\ p_1\ ,\ ..\ ,\ l_n\ =\ p_n\,\} & & \mathrm{b} = \mathrm{b}(p_1..p_n)
\end{array}
$$

metavars *metavarroot*, *mvr* *nontermroot*, *ntr*
terminal, *t* *auxfn*, *f*
prodname, *pn* *variable*, *var*

grammar

metavar, *mv* ::=
| *metavarroot suffix*

nonterm, *nt* ::=
| *nontermroot suffix*

element, *e* ::=
| *terminal*
| *metavar*
| *nonterm*

metavar_set_expression, *mse* ::=
| *metavar*
| *auxfn*`(`*nonterm*`)`
| *mse* `union` *mse′*
| {}

bindspec, *bs* ::=
| `bind` *mse* `in` *nonterm*
| *auxfn* = *mse*

prod, *p* ::=
| `|` *element*$_1$ .. *element*$_m$ `::` *prodname* `(+` *bs*$_1$ .. *bs*$_n$ `+)`

rule, *r* ::=
| *nontermroot* `::` `''` `::=` *prod*$_1$ .. *prod*$_m$

grammar_rules, *g* ::=
| `grammar` *rule*$_1$ .. *rule*$_m$

Figure 12: Mini-Ott in Ott: the binding specification metalanguage

This suffices to express the binding structure of almost all the natural examples we have come across, including definitions of mutually recursive functions with multiple clauses for each, Join calculus definitions [FGL+96], dependent record patterns, and many others.

10 Generating substitution and free variable functions

The tool can generate Isabelle/Coq/HOL/OCaml code for both single and multiple substitution functions. For example, the ML polymorphism Ott source of `test8.ott` includes the following.

```
substitutions
  single   expr value_name :: subst
  multiple typexpr typvar  :: tsubst
```

This causes the generation of two families of substitution functions, one replacing a single `value_name` by a `expr`, the other replacing multiple `typvar`s by `typexpr`s.

Each family contains a function for each datatype for which it is required, so in that example there are functions `subst_expr` for the first and `tsubst_typexpr`, `tsubst_typscheme` and `tsubst_G` for the second.

The functions for substitutions declared by

```
substitutions
  single   this that :: name1
  multiple this that :: name2
```

replaces terms of productions consisting just of a single `that` by a `this`. Here `this` must be a nonterminal root, while `that` can be either a metavariable root or a nonterminal root (the latter possibility allows substitution for compound identifiers, though it is not clear that this is generally useful enough to be included). Substitution functions are generated for each member of each (mutually recursive) block of grammar rules which either contain such a production or (indirectly) refer to one that does.

At present multiple substitutions are represented by Isabelle/Coq/HOL/OCaml lists, so for the example above we have Isabelle

```
tsubst_typexpr :: "(typvar*typexpr) list => typexpr => typexpr"
tsubst_typscheme :: "(typvar*typexpr) list => typscheme => typscheme"
tsubst_G :: "(typvar*typexpr) list => G => G"
```

The generated functions do not substitute bound things, and recursive calls under binders are filtered to remove the bound things.

Similarly, the tool can generate Isabelle/Coq/HOL/OCaml to calculate the free variables of terms. For example, the ML polymorphism Ott source of `test8.ott` includes the following.

```
freevars
  typexpr typvar :: ftv
```

This causes Isabelle functions as below to be generated, calculating the free `typvar`s that occur in singleton productions in the `typexpr` grammar, within terms of all types.

```
ftv_typexpr :: "typexpr => typvar list"
ftv_typscheme :: "typscheme => typvar list"
ftv_G :: "G => typvar list"
```

11 List forms

Ott has direct support for lists, both as *dot forms* such as $t_1, \ldots, t_n$ and as *list comprehensions* such as $\overline{t_i}^{\,i \in 1..n}$. Figure 13 shows an example semantic rule taken from our OCaml fragment semantics, as both the generated LaTeX and its Ott source, that involves several dot forms. Other types commonly used in semantics, e.g. finite maps or sets, can often be described with this list syntax in conjunction with type and metaproduction homs to specify the proof assistant representation. When using list forms, one usually also wants to add a list-of-formula production to the **formula** grammar, e.g. (as in `test17.10.ott`):

```
formula :: formula_ ::=
  |  judgement                    ::   :: judgement
  |  formula1 .. formulan         ::   :: dots
```

The proof assistant code generation for such a production (which must be named `formula_dots`) is special-cased to a list conjunction.

11.1 List dot forms

Example productions for record types, record terms, and record patterns are shown below, in both Ott source and LaTeX, taken from our $F_{<:}$ example.

```
T, S, U :: 'T_' ::=                                                {{ com type  }}
  | { l1 : T1 , .. , ln : Tn }      :: :: Rec                        {{ com record }}

t :: 't_' ::=                                                      {{ com  term  }}
  | { l1 = t1 ,  .. , ln = tn }     :: :: Rec                        {{ com record }}
  | let p = t in t'                 :: :: Let (+ bind b(p) in t' +) {{ com pattern binding}}

p :: 'P_' ::=                                                      {{ com  pattern }}
  | x : T                           :: :: Var (+ b = x  +)           {{ com variable pattern }}
```

$$\frac{\begin{array}{l} E \vdash e_1 : t_1 \quad ... \quad E \vdash e_n : t_n \\ E \vdash field\_name_1 : t \to t_1 \quad ... \quad E \vdash field\_name_n : t \to t_n \\ t = (\, t'_1 \,, \ldots \,, t'_l \,)\ typeconstr\_name \\ E \vdash typeconstr\_name \ \rhd \ typeconstr\_name : kind\, \{\, field\_name'_1 \,; \ldots \,; field\_name'_m \,\} \\ field\_name_1 \ldots field\_name_n \ \textbf{PERMUTES}\ field\_name'_1 \ldots field\_name'_m \\ \textbf{length}\,(\, e_1 \,) \ldots (\, e_n \,) \geq 1 \end{array}}{E \vdash \{\, field\_name_1 = e_1 \,; \ldots \,; field\_name_n = e_n \,\} : t} \quad \textsc{JTe\_record\_constr}$$

```
E |- e1 : t1 ... E |- en : tn
E |- field_name1 : t->t1 ... E |- field_namen : t->tn
t = (t1', ..., tl') typeconstr_name
E |- typeconstr_name gives typeconstr_name:kind {field_name1'; ...; field_namem'}
field_name1...field_namen PERMUTES field_name1'...field_namem'
length (e1)...(en)>=1
------------------------------------------------------------------------ :: record_constr
E |- {field_name1=e1; ...; field_namen=en} : t
```

Figure 13: A sample OCaml semantic rule, in LaTeX and Ott source forms

```
| { l1 = p1 , .. , ln = pn }      :: :: Rec (+ b = b(p1 .. pn) +) {{ com  record pattern  }}
```

$T,\ S,\ U$	::=			type
	|	$\{\, l_1 : T_1 \,, .. \,, l_n : T_n \,\}$		record
t	::=			term
	|	$\{\, l_1 = t_1 \,, .. \,, l_n = t_n \,\}$		record
	|	$\textbf{let}\ p = t\ \textbf{in}\ t'$	$\mathsf{bind}\ \mathrm{b}(p)\ \mathsf{in}\ t'$	pattern binding
p	::=			pattern
	|	$x : T$	$\mathrm{b} = x$	variable pattern
	|	$\{\, l_1 = p_1 \,, .. \,, l_n = p_n \,\}$	$\mathrm{b} = \mathrm{b}(p_1 .. p_n)$	record pattern

Dot forms can be used in symbolic terms in semantic rules:

$$\frac{\Gamma \vdash t_1 : T_1 \quad .. \quad \Gamma \vdash t_n : T_n}{\Gamma \vdash \{\, l_1 = t_1 \,, .. \,, l_n = t_n \,\} : \{\, l_1 : T_1 \,, .. \,, l_n : T_n \,\}} \quad \textsc{Ty\_Rcd}$$

Individually indexed projections from dot forms can be mentioned, eg the l_j below:

$$\frac{\Gamma \vdash t : \{\, l_1 : T_1 \,, .. \,, l_n : T_n \,\}}{\Gamma \vdash t\,.\,l_j : T_j} \quad \textsc{Ty\_Proj}$$

Symbolic terms can also include concatenations of two dot forms with a singleton in between:

$$\frac{t \longrightarrow t'}{\{\, l_1 = v_1 \,, .. \,, l_m = v_m \,,\ l = t \,,\ l'_1 = t'_1 \,, .. \,, l'_n = t'_n \,\} \longrightarrow \{\, l_1 = v_1 \,, .. \,, l_m = v_m \,,\ l = t' \,,\ l'_1 = t'_1 \,, .. \,, l'_n = t'_n \,\}} \quad \textsc{reduce\_Ctx\_record}$$

Multiple dot forms within the same semantic rule can share bounds (e.g. $1..m$):

$$\frac{\forall i \in 1..m . \exists j \in 1..n . (\, l_i = k_j \ \wedge\ \textbf{match}\,(\, p_i \,,\ v_j \,) = \sigma_i \,)}{\textbf{match}\,(\, \{\, l_1 = p_1 \,, .. \,, l_m = p_m \,\} \,, \{\, k_1 = v_1 \,, .. \,, k_n = v_n \,\} \,) = \sigma_1 \,, .. \,, \sigma_m} \quad \textsc{M\_Rcd}$$

In more detail, productions can have dot tokens interspersed between the elements. Dot tokens consist of two, three or four consecutive dots (.., ..., or ....), indicating lists with minimum lengths 0, 1,

and 2 respectively (these length minimums are respected only when parsing concrete lists; they are not present in Isabelle/Coq/HOL output). The tool identifies the maximal sequence of elements on either side of the dots that are identical modulo anti-unification of some index. Optionally, there may also be a single terminal on either side of the dot token, separating instances of the repeated unit. For example, in the `test7.ott` production

```
| { l1 = t1 ,  .. , ln = tn }  :: :: Rec
```

there is such a terminal (the ','). The tool identifies that `l1 = t1` and `ln = tn` can be anti-unified as (roughly) `l_ = t_`, taking `_` to be the bounds `1` and `n`. A single production may contain multiple dot forms, but they must not overlap; nested dot forms (including those with multiple changing indices) are not currently supported.

Homomorphisms and binding specifications are generalised to match: an `mse` can involve a dot form of metavariables; a dot form of nonterminals; or an auxiliary function applied to a dot form of nonterminals (e.g. the b(p_1..p_n) above). Dot forms on the right of a **`bind`** are not currently supported.

LaTeX homomorphisms should not refer to dot forms, as either an error or bad output will be generated. (For LaTeX, there should really be some means to specify a homomorphism for the repeated expression, and also data on how any list separators should be typeset. This would require more special-case treatment, which is not currently supported.)

11.2 List comprehension forms

Lists can also be expressed as explicit list comprehensions, for more concise typesetting. Three different styles are supported, with no bounds, an upper bound, or a lower and upper bound. For example, in a symbolic term, instead of the dot form

```
G |- t1:T1  ..  G |- tn:Tn
```

one can write any of the following

```
</ G |- ti:Ti // i           />
</ G |- ti:Ti // i IN n      />
</ G |- ti:Ti // i IN 1 .. n />
```

Similar comprehensions can be used in productions, for example lines 2–4 below. In addition, comprehensions in productions can specify a terminal to be used as a separator in concrete lists, as in lines 5–7 below. (These examples are taken from `test17.10.ott`.)

```
|  l1 = t1 ,  .. , ln = tn            :: :: Rec              {{ com dots }}
|  </ li = ti // i           />       :: :: Rec_comp_none    {{ com comp }}
|  </ li = ti // i IN n      />       :: :: Rec_comp_u_none  {{ com compu }}
|  </ li = ti // i IN 1 .. n />       :: :: Rec_comp_lu_none {{ com complu }}
|  </ li = ti // , // i           />  :: :: Rec_comp_some    {{ com comp with terminal }}
|  </ li = ti // , // i IN n      />  :: :: Rec_comp_u_some  {{ com compu with terminal }}
|  </ li = ti // , // i IN 1 .. n />  :: :: Rec_comp_lu_some {{ com complu with terminal }}
```

In Coq, HOL or Isabelle output, list dot forms and the various list comprehension forms are treated almost identically. In LaTeX output, comprension forms are default-typeset with overbars. For example, the rules below

```
G|- t:l1:T1,..,ln:Tn
---------------------- :: Proj_dotform
G|- t.lj : Tj

G|- t:  </ li:Ti // i/>
--------------------------------- :: Proj_comp
G|- t.lj : Tj

G|- t:  </ li:Ti // i IN n/>
```

```
---------------------------------- :: Proj_comp_u
G|- t.lj : Tj

G|- t:  </ li:Ti // i IN 1..n/>
---------------------------------- :: Proj_comp_lu
G|- t.lj : Tj
```

are typeset as follows.

$$\frac{\Gamma \vdash t : \{\, l_1 : T_1 \,,\, .. \,,\, l_n : T_n \,\}}{\Gamma \vdash t\,.\,l_j \;:\; T_j} \quad \textsc{Ty\_Proj\_dotform}$$

$$\frac{\Gamma \vdash t : \{\, \overline{l_i : T_i}^{\,i} \,\}}{\Gamma \vdash t\,.\,l_j \;:\; T_j} \quad \textsc{Ty\_Proj\_comp}$$

$$\frac{\Gamma \vdash t : \{\, \overline{l_i : T_i}^{\,i<n} \,\}}{\Gamma \vdash t\,.\,l_j \;:\; T_j} \quad \textsc{Ty\_Proj\_comp\_u}$$

$$\frac{\Gamma \vdash t : \{\, \overline{l_i : T_i}^{\,i\in 1..n} \,\}}{\Gamma \vdash t\,.\,l_j \;:\; T_j} \quad \textsc{Ty\_Proj\_comp\_lu}$$

Upper bounds of the form $n-1$ are also permitted, e.g. with

```
G|- t:l0:T0,..,ln-1:Tn-1
------------------------ :: Proj_dotform_minus
G|- t.lj : Tj

G|- t:  </ li:Ti // i IN 0..n-1/>
---------------------------------- :: Proj_comp_lu_minus
G|- t.lj : Tj
```

typeset as below. More complex arithmetic expressions are not currently supported.

$$\frac{\Gamma \vdash t : \{\, l_0 : T_0 \,,\, .. \,,\, l_{n-1} : T_{n-1} \,\}}{\Gamma \vdash t\,.\,l_j \;:\; T_j} \quad \textsc{Ty\_Proj\_dotform\_minus}$$

$$\frac{\Gamma \vdash t : \{\, \overline{l_i : T_i}^{\,i\in 0..n-1} \,\}}{\Gamma \vdash t\,.\,l_j \;:\; T_j} \quad \textsc{Ty\_Proj\_comp\_lu\_minus}$$

A list form used in a symbolic term does not have to be in the same style as that in the corresponding production. However, if a metavariable or nonterminal occurs in multiple different list forms in the same inference rule, they must all be in the same style and with the same bounds. Moreover, in a production, a list form in a bindspec or homomorphism must be in the same style and with the same bounds as the corresponding list form in the elements of the production.

The comprehension form without an upper bound, e.g. `</ G |- ti:Ti // i />`, typeset as $\overline{\Gamma \vdash t_i : T_i}^{\,i}$, is not standard notation, but is often very useful. Many semantic rules involve lists of matched length, e.g. of the t_i and T_i here, but do not need to introduce an identifier for that length; omitting it keeps them concise.

The default visual style for typesetting list comprehensions can be overridden by redefining the LaTeX commands `\ottcomp`, `\ottcompu`, and `\ottcomplu` in an **embed** section, as in Section 4.3.

In some cases one could make the typeset notation even less noisy, by either omitting the superscript i or omitting both the superscript i and the subscript i's on t and T. The first is unambiguous if there is at most one index on each element in the comprehension; the second if all the elements are indexed by the same thing (not the case for this example, but common for comprehensions of single elements,

e.g. `<< Ti // i>>` for $\overline{T}$). It is arguable that that should be automated in future Ott releases, though it would bring the typeset and ASCII versions out of step.

List comprehension forms can also be used in bindspecs and in homomorphisms.

11.3 Proof assistant code for list forms

11.3.1 Types

We have to choose proof assistant representations for productions involving list forms. For example, for a language with records one might write

```
metavar label, l ::= {{ hol string }} {{ coq nat }}
indexvar index, n ::=  {{ hol num }} {{ coq nat }}
grammar
t :: E_ ::=
  | { l1 = t1 ,  .. , ln = tn }      :: :: record
```

In HOL and Isabelle we represent these simply with contructors whose argument types involve proof-assistant native list types, e.g. the HOL list of pairs of a `label` and a `t`:

```
val _ = Hol_datatype `
t = E_record of (label#t) list  `;
```

For Coq we provide two alternatives: one can either use native lists, or lists can be translated away, depending on taste. The choice is determined by the `-coq_expand_list_types` command-line option. In the former case we generate an appropriate induction principle using nested fixpoints, as the default principle produced by Coq is too weak to be useful. In the latter case we synthesise an additional type for each type of lists-of-tuples that arises in the grammar. In the example, we need a type of lists of pairs of a `label` and a `t`:

```
Inductive
list_label_t : Set :=
   Nil_list_label_t : list_label_t
 | Cons_list_label_t : label -> t -> list_label_t
     -> list_label_t

with t : Set :=
   E_record : list_label_t -> t .
```

These are included in the topological sort, and utility functions, e.g. to make and unmake lists, are synthesised.

11.3.2 Terms (in inductive definition rules)

Supporting list forms in the rules of an inductive definition requires some additional analysis. For example, consider the record typing rule below.

$$\frac{\Gamma \vdash t_0 : T_0 \quad .. \quad \Gamma \vdash t_{n-1} : T_{n-1}}{\Gamma \vdash \{ l_0 = t_0 , .. , l_{n-1} = t_{n-1} \} : \{ l_0 : T_0 , .. , l_{n-1} : T_{n-1} \}} \quad \textsc{Ty\_Rcd}$$

We analyse the symbolic terms in the premises and conclusion to identify lists of nonterminals and metavariables with the same bounds — here $t_0..t_{n-1}$, $T_0..T_{n-1}$, and $l_0..l_{n-1}$ all have bounds $0..n-1$. To make the fact that they have the same length immediate in the generated code, we introduce a single proof assistant variable for each such collection, with appropriate projections and list maps/foralls at the usage points. For example, the HOL for the above is essentially as follows, with an `l_t_Typ_list : (label#t#Typ) list`.

```
(* Ty_Rcd *)  !(l_t_Typ_list:(label#t#Typ) list) (G:G) .
(EVERY (\b.b)
  (MAP (\(l_,t_,Typ_). (Ty G t_ Typ_)) l_t_Typ_list))
 ==>
(Ty
  G
  (E_record (MAP (\(l_,t_,Typ_). (l_,t_)) l_t_Typ_list))
  (T_Rec    (MAP (\(l_,t_,Typ_). (l_,Typ_)) l_t_Typ_list)))
```

This seems to be a better idiom for later proof development than the alternative of three different list variables coupled with assertions that they have the same length.

With direct support for lists, we need also direct support for symbolic terms involving list projection and concatenation. For example, the rule

$$\frac{t \longrightarrow t'}{\begin{array}{l}\{\, l_1 = v_1\,,\, ..\,,\, l_m = v_m\,,\, l = t\,,\, l'_1 = t'_1\,,\, ..\,,\, l'_n = t'_n\,\} \\ \longrightarrow \{\, l_1 = v_1\,,\, ..\,,\, l_m = v_m\,,\, l = t'\,,\, l'_1 = t'_1\,,\, ..\,,\, l'_n = t'_n\,\}\end{array}} \quad \textsc{Rec}$$

gives rise to HOL code as below — note the list-lifted usage of the `is_v_of_t` predicate, and the list appends (`++`) in the conclusion.

```
(* reduce_Rec *)  !(l'_t'_list:(label#t) list)
       (l_v_list:(label#t) list) (l:label) (t:t) (t':t) .
((EVERY (\(l_,v_). is_v_of_t v_) l_v_list) /\
(( reduce t t' )))
 ==>
(( reduce (t_Rec (l_v_list ++ [(l,t)] ++ l'_t'_list))
          (t_Rec (l_v_list ++ [(l,t')] ++ l'_t'_list))))
```

For the `Proj` typing rule

$$\frac{\Gamma \vdash t : \{\, \overline{l_i : T_i}^{\,i \in 0..n-1} \,\}}{\Gamma \vdash t\,.\,l_j \,:\, T_j} \quad \textsc{Proj}$$

we need a specific projection (the HOL `EL`) to pick out the j'th element:

```
(* Ty_Proj *)  !(l_Typ_list:(label#Typ) list)
       (j:index) (G:G) (t:t) .
((( Ty G t (T_Rec (l_Typ_list)) )))
 ==>
(( Ty
     G
     (t_Proj t  ((\ (l_,Typ_) . l_) (EL j l_Typ_list)))
     ((\ (l_,Typ_) . Typ_) (EL  j l_Typ_list))))
```

For Coq, when translating away lists, we have to introduce yet more list types for these proof assistant variables, in addition to the obvious translation of symbolic terms, and, more substantially, to introduce additional inductive relation definitions to induct over them.

For similar examples in Isabelle, the generated Isabelle for the first three rules of §11.1 is shown below (lightly hand-edited for format). The first involves an Isabelle variable `l_t_T_list`, and list maps and projections thereof.

```
Ty_RcdI: "
  [|(formula_formuladots ((List.map (%(l_,t_,T_).( ( G , t_ , T_ ) : Ty)) l_t_T_list)))|]
  ==>
  ( G ,
    (t_Rec ((List.map (%(l_,t_,T_).(l_,t_)) l_t_T_list))) ,
    (T_Rec ((List.map (%(l_,t_,T_).(l_,T_)) l_t_T_list)))
  ) : Ty"

Ty_ProjI: "
```

```
  [| ( G , t , (T_Rec (l_T_list)) ) : Ty|] ==>
  ( G ,
    (t_Proj t (%(l_,T_).l_) (List.nth l_T_list (j - 1))) ,
    (%(l_,T_).T_) (List.nth l_T_list (j - 1))
  ) : Ty"

E_Ctx_recordI: "
[| List.list_all (%(l_,v_).is_v v_) l_v_list ;
   ( t , t' ) : E|]
==>
 ( (t_Rec (l_v_list @ [(l,t)] @ l_'t_'list)) ,
   (t_Rec (l_v_list @ [(l,t')] @ l_'t_'list))
 ) : E"
```

The generated code for substitutions and free variables takes account of such list structure.

Note that at present the generated Isabelle code for these functions does not always build without change, in particular if tuples of size 3 or more are required in patterns.

11.3.3 List forms in homomorphisms

Proof assistant homomorphisms in productions can refer to dot-form metavariables and nonterminals. For example, the second production below (taken from `test17.9`) mentions `[[x1 t1 ... xn tn]]` in the **isa** homomorphism. This must exactly match the dot form in the production except that all terminals must be omitted — the metavariables and nonterminals must occur in the same order as in the production, and the bounds must be the same.

```
    E :: 'E_' ::= {{ isa ( ident * t ) list  }}
      | < x1 : t1 , .. , xn : tn > :: :: 2  {{ isa  List.rev [[x1 t1 .. xn tn]] }}
    formula :: formula_ ::=
      | judgement              :: :: judgement
      | formula1 .. formulan   :: :: dots
```

The generated Isabelle code for symbolic terms mentioning this production will involve a list of pairs. For example, the rules

```
defn
|- E  :: :: Eok :: Eok_ by

---------------------------- :: 2
|- <x1:t1,..,xn:tn>

|- t1:K1  .. |- tn:Kn
---------------------------- :: 3
|- <x1:t1,..,xn:tn>
```

generate

```
consts
  Eok :: "E set"
inductive Eok tK
intros

(* defn Eok *)

Eok_2I: " ( List.rev  (x_t_list) ) : Eok"

Eok_3I: "[|
(List.list_all (\<lambda> b . b) (  ((List.map (%(x_,t_,K_). ( t_ , K_ ) : tK) x_t_K_list))  ) )|]
 ==>
 ( List.rev  ((List.map (%(x_,t_,K_).(x_,t_)) x_t_K_list)) ) : Eok"
```

Note that in the second the list of pairs is projected out from the `x_t_K_list` list of triples that is quantified over in the rule.

12 Subrules

Subrule declarations have the form

```
subrules
  nt1 <:: nt2
```

where `nt1` and `nt2` are nonterminal roots.

Subrules can be chained, i.e. there can be a pair of subrule declarations `nt1 <:: nt2` and `nt2 <:: nt3`, and they can form a directed acyclic graph, e.g. with `nt0 <:: nt1`, `nt0 <:: nt2`, `nt1 <:: nt3`, and `nt2 <:: nt3`. However, there cannot be cycles, or nonterminal roots for which there are multiple upper bounds. Subrule declarations should not involve nonterminal roots for which proof-assistant type homs are specified.

We support the case in which the upper rule is also non-free, i.e. it contains productions that mention nonterminals that occur on the left of a subrule declaration. In the example below (`test11.ott`) the `t` rule contains a production `Foo v`.

```
metavar termvar , x ::=
  {{ isa string }} {{ coq nat }} {{ coq-equality }} {{ hol string }} {{ ocaml int }}

grammar
  t :: 't_' ::=
    | x                    ::   :: Var
    | \ x . t              ::   :: Lam  (+ bind x in t +)
    | t t'                 ::   :: App
    | Foo v                ::   :: Foo

  v :: 'v_' ::=
    | \ x . t              ::   :: Lam

subrules
  v <:: t

defns
  Jb :: '' ::=

    defn
    Baz t , v ::  :: Baz :: ''      by


    --------- :: ax
    Baz t , v
```

In this case generated Isabelle/Coq/HOL/OCaml will define a single type and both `is_v` and `is_t` predicates, and the generated inductive definition clause for `ax` uses both predicates. The Isabelle clause is below.

```
axI: "[|is_t t ; is_v v|] ==>  ( t , v ) : Baz"
```

13 Context rules

The system supports the definition of single-hole contexts, e.g. for evaluation contexts. For example, suppose one has a term grammar as below:

```
t :: 't_' ::=                                {{ com term    }}
  | x                  ::  :: Var                  {{ com variable}}
  | \ x . t            ::  :: Lam (+ bind x in t +) {{ com lambda  }}
  | t t'               ::  :: App                  {{ com app     }}
  | ( t1 , .... , tn ) ::  :: Tuple                {{ com tuple }}
  | ( t )              :: S:: Paren                {{ icho [[t]]  }}
  | { t / x } t'       :: M:: Tsub
                       {{ icho (tsubst_t [[t]] [[x]] [[t']])}}

  | E . t              :: M:: Ctx
                       {{ icho (appctx_E_t [[E]] [[t]])}}
                       {{ tex [[E]] \cdot [[t]] }}
```

A context grammar is declared as a normal grammar but with a single occurrence of the terminal `__` in each production, e.g. as in the grammar for `E` below (a rather strange evaluation strategy, admittedly).

```
E :: 'E_' ::=                                {{ com evaluation context }}
  | __ t          ::  :: AppL                   {{ com app L    }}
  | v __          ::  :: AppR                   {{ com app R    }}
  | \ x . __      ::  :: Lam                    {{ com reduce under lambda }}
  | ( t1 ( __  t2 ) ) :: :: Nested               {{ com hole nested }}
  | ( v1 , .. , vm , __ , t1 , .. , tn ) :: :: Tuple {{ com tuple }}
```

A **contextrules** declaration:

```
contextrules
  E _:: t :: t
```

causes Ott to (a) check that each production of the `E` grammar is indeed a context for the `t` grammar, and (b) generates proof assistant functions, e.g. `appctx_E_t`, to apply a context to a term:

```
(** context application *)
Definition appctx_E_t (E5:E) (t_6:t) : t :=
  match E5 with
  | (E_AppL t5) => (t_App t_6 t5)
  | (E_AppR v5) => (t_App v5 t_6)
  | (E_Lam x) => (t_Lam x t_6)
  | (E_Nested t1 t2) =>  (t_App t1  (t_App t_6 t2) )
  | (E_Tuple v_list t_list) => (t_Tuple ((app_list_t v_list
     (app_list_t (Cons_list_t t_6 Nil_list_t) (app_list_t t_list Nil_list_t)))))
```

As the `Nested` production shows, context productions can involve nested term structure.

Note also that here the `E` grammar is not free (it mentions the subrule nonterminal `v`) so an isvalue predicate `is_E_of_E` is also generated.

In general, context rule declarations have the form

```
contextrules
  ntE _:: nt1 :: nt2
```

where `ntE`, `nt1`, and `nt2` are nonterminal roots. This declares contexts `ntE` for the `nt1` grammar, with holes in `nt2` positions.

Just as for substitutions, the context application function is typically used by adding a metaproduction to the term grammar. Here we add a production `E.t` to the `t` grammar with an `icho` hom that uses `appctx_E_t`.

```
t :: 't_' ::=                                {{ com term    }}
  ...
  | E . t              :: M:: Ctx
                       {{ icho (appctx_E_t [[E]] [[t]])}}
                       {{ tex [[E]] \cdot [[t]] }}
```

That can then be used in relations:

```
t --> t'
-------------- :: ctx
E.t --> E.t'
```

One would typically also define a `terminals` production for the hole terminal `__`, e.g. here we typeset the hole as $[\cdot]$.

```
terminals :: 'terminals_' ::=
  | __           ::  :: hole    {{ tex [\cdot] }}
```

14 Parsing Priorities

Symbolic terms that can have more than one parse tree are typically considered erroneous; however, certain classes of parse trees are ignored in order to support common idioms that are ambiguous. For example, the production

$$\Gamma ::= \Gamma_1, .., \Gamma_n$$

might be used to allow a list of typing contexts to be appended together, but it is highly ambiguous. The following restrictions forbid many unwanted parses that could otherwise occur.

- All parses in which a nonterminal derives itself without consuming any input are ignored. For example, in the production above, the list could otherwise be of length one so that Γ directly derives Γ giving rise to a vacuous cycle, and an infinite forest of parse trees. This restriction ensures that only the tree without the vacuous cycle is considered.
- The parser for a list form ignores parses that unnecessarily break up the list due to (direct or indirect) self reference. For example, $\Gamma_1, \Gamma_2, \Gamma_3, \Gamma_4$ will not parse as a two element sequence of two element sequences $(\Gamma_1, \Gamma_2), (\Gamma_3, \Gamma_4)$ given the production above.
- User supplied priority annotations in a **parsing** section rule out certain trees as follows:
  - *prodname*$_1$ `<=` *prodname*$_2$: Parse trees where a *prodname*$_1$ node is a child of a *prodname*$_2$ node are ignored.
  - *prodname*$_1$ **right** *prodname*$_2$: Parse trees where a *prodname*$_1$ node is the leftmost child of a *prodname*$_1$ node are ignored.
  - *prodname*$_1$ **left** *prodname*$_2$: Parse trees where a *prodname*$_2$ node is the rightmost child of a *prodname*$_1$ node are ignored.

  In addition to immediate children, these priority annotations also prohibit parse trees where the forbidden child node occurs underneath a chain of derivations from the specified parent when the chain does not consume any input. Figure 14 demonstrates a typical use of a **parsing** section; the declarations have effect as follows:
  - Line #1: `n + n + n` parses as `(n + n) + n`, but not `n + (n + n)`;
  - Line #3: `n + n - n` parses as `(n + n) - n`, but not `n + (n - n)`;
  - Line #9: `-n + n` parses as `(-n) + n`, but not `-(n + n)`;
  - Line #15: `n + n n` parses as `n + (n n)`, but not `(n + n) n`; `n n + n` parses as `(n n) + n`, but not `n (n + n)`;
  - Line #20: `n, n n, n` parses as `n, (n n), n`, but not `(n, n) (n, n)`.

  Currently, the **parsing** section supports only these relatively low level and verbose declarations.

```
metavar n ::=

grammar

e :: e_ ::=
| n              ::   :: num
| - e            ::   :: neg
| e1 + e2        ::   :: add
| e1 - e2        ::   :: sub
| e1 e2          ::   :: mul
| e1 / e2        ::   :: div
| e1 , .. , e2   ::   :: tup
| ( e )          :: M :: par {{ icho [[e]] }}

parsing

e_add left e_add   % #1
e_sub left e_sub
e_add left e_sub   % #3
e_sub left e_add

e_mul left e_mul
e_div left e_div
e_mul left e_div
e_div left e_mul

e_neg <= e_add     % #9
e_neg <= e_sub
e_neg <= e_mul
e_neg <= e_div
e_neg <= e_tup

e_add <= e_div
e_add <= e_mul     % #15
e_add <= e_tup
e_sub <= e_div
e_sub <= e_mul
e_sub <= e_tup

e_mul <= e_tup     % #20
e_div <= e_tup
```

Figure 14: An Ott source file for basic arithmetic using the typical parsing priorities

```
grammar
t :: Tm ::=                                              {{ com terms: }}
  | let x = t in t'                    ::   :: Let (+ bind x in t' +)     {{ com let binding }}


defns
Jop :: '' ::=

defn
t --> t' :: :: red :: E_ {{ com Evaluation }} by

------------------------------ :: LetV
let x=v1 in t2 --> [x|->v1]t2

t1 --> t1'
---------------------------------- :: Let
let x=t1 in t2 --> let x=t1' in t2


defns
Jtype :: '' ::=

defn
G |- t : T :: :: typing :: T_ {{ com Typing }} by

G |- t1:T1
G,x:T1 |- t2:T2
------------------------ :: Let
G |- let x=t1 in t2 : T2
```

Figure 15: An `ott` source file for the `let` fragment of TAPL

15 Combining multiple Ott source files

If Ott is invoked with multiple source files on the command line, they are usually processed as if they were simply concatenated. If, however, one adds a `-merge true` command-line option then the productions of multiple grammars that share the same header are merged into a single grammar, and the rules of multiple inductive definitions that share the same header are merged into a single inductive definition.

This rudimentary form of modularity can be very useful, either to split a language definition into separate features, or to define reusable Ott components to define standard formulae, LaTeX pretty printing of terminals, or LaTeX styles. For example, Figure 15 shows the Ott source file for a `let` feature in isolation, taken from our Ott development of some languages from Pierce's TAPL [Pie02]. The original TAPL languages were produced using TinkerType [LP03] to compose features and check for conflicts. In `examples/tapl` we build a system, similar to the TinkerType `sys-fullsimple`, from `ott` source files that correspond roughly to the various TinkerType components, each with syntax and semantic rules for a single feature.

16 Hom blocks

Bindspecs and homomorphisms for productions, and any homomorphisms for definitions, can appear in an Ott source file either attached to the production or definition, as we have shown earlier, or in separate hom blocks. For example, one can write

```
homs 't_'
  :: Lam  (+ bind x in t +)

homs 't_'
```

```
  :: Var     {{ com variable }}
  :: Lam     {{ com abstraction }}
  :: App     {{ com application }}
  :: paren   {{ ich [[t]] }}
  :: tsub    {{ ich ( tsubst_t [[t]] [[x]] [[t']] ) }}

homs ''
  :: reduce  {{ com [[t1]] reduces to [[t2]] }}
```

Each of these begins with a prefix and then has a sequence of production name or definition name kernels, each followed by a sequence of bindspecs and then a sequence of homomorphisms.

The `test10_homs.ott` example, in Fig. 16, shows this. It is semantically equivalent to the `test10.ott` example of Fig. 8, but the homs have been moved into `hom` blocks.

17 Isabelle syntax support

Ott has limited facilities to allow the Isabelle mixfix syntax support and xsymbol to be used. The example `test10_isasyn.ott` shows this in use.

Non-meta productions can be annotated with **isasyn** and/or **isaprec** homomorphisms. For example, `test10_isasyn.ott` contains the production

```
  | t t'      :: :: App   {{ isasyn [[t]]\<bullet>[[t']] }}  {{ isaprec 50 }}
```

The two homs are used to output the Isabelle syntax annotation in the `t_App` clause of the datatype definition below.

```
t =
   t_Var "termvar"
 | t_Lam "termvar" "t"  ("\<lambda> _ . _" 60)
 | t_App "t" "t"  ("_\<bullet>_" 50)
```

Definitions can be annotated with **isasyn** and/or **isaprec** homomorphisms similarly, e.g. as below.

```
    defn
    t1 --> t2 ::  :: reduce :: '' {{ isasyn [[t1]] ---> [[t2]] }}  by
```

This generates `syntax` and `translations` blocks as below.

```
inductive_set reduce :: "(t*t) set"
and  "reduce'" :: "t => t =>  bool" ("_ ---> _" 50)
where "(t1 ---> t2) ==  ( t1 , t2 ) : reduce"
```

Symbolic terms in definitions are printed using any production or definition syntax. This (especially with xsymbol turned on) makes the current goal state during Isabelle proof development much more readable.

Further, there is a command line option `-isa_syntax true`. If this is set then the tool generates Isabelle syntax annotations from the source syntax. For example, the source file production for the `t_Lam` clause is

```
    | \ x . t              ::   :: Lam   {{ isaprec 60 }}
```

and the `terminals` grammar contains a mapping from `\` to `\<lambda>`:

```
  terminals :: 'terminals_' ::=
    | \                    ::   :: lambda  {{ tex \lambda }}  {{ isa \<lambda> }}
    | -->                  ::   :: red     {{ tex \longrightarrow }} {{ isa ---> }}
```

This is used (just as for LaTeX homs) to generate the `("\<lambda> _ . _" 60)` in the datatype definition above.

This functionality is limited in various ways: (1) the full range of Isabelle precedence and associativity specifications are not supported; (2) the automatically generated syntax annotations are somewhat crude,

```
metavar termvar , x ::=
  {{ isa string }} {{ coq nat }} {{ coq-equality }} {{ hol string }} {{ lex alphanum }}
  {{ tex \mathit{[[termvar]]} }} {{ com  term variable  }}

grammar
  t :: 't_' ::=    {{ com term }}
    | x                      ::   :: Var
    | \ x . t                ::   :: Lam
    | t t'                   ::   :: App
    | ( t )                  :: S :: paren
    | { t / x } t'           :: M :: tsub

  v :: 'v_' ::=    {{ com  value }}
    | \ x . t                ::   :: Lam

  terminals :: 'terminals_' ::=
    | \                      ::   :: lambda  {{ tex \lambda }}
    | -->                    ::   :: red     {{ tex \longrightarrow }}


homs 't_'
  :: Lam  (+ bind x in t +)

homs 't_'
  :: Var     {{ com variable }}
  :: Lam     {{ com abstraction }}
  :: App     {{ com application }}
  :: paren   {{ ich [[t]] }}
  :: tsub    {{ ich ( tsubst_t [[t]] [[x]] [[t']] ) }}

homs ''
  :: reduce  {{ com [[t1]] reduces to [[t2]] }}


subrules
  v <:: t

substitutions
  single t x :: tsubst

defns
  Jop :: '' ::=

    defn
    t1 --> t2 ::  :: reduce :: '' by


    ---------------------------  :: ax_app
    (\x.t12) v2 -->  {v2/x}t12

    t1 --> t1'
    -------------- :: ctx_app_fun
    t1 t --> t1' t

    t1 --> t1'
    -------------- :: ctx_app_arg
    v t1 --> v t1'
```

Figure 16: Hom Sections: `test10_homs.ott`

especially w.r.t. spacing and parenthesisation; (3) syntax annotation on meta productions is not propertly supported; and (4) it would be desirable to have more fine-grain control of whether to automatically generate annotations: per-production, per-rule, and per-file.

18 Isabelle code generation example

The Isabelle/Coq/HOL code generation facilities can be sometimes used to generate (variously) OCaml and SML code from the Isabelle/Coq/HOL definitions produced by Ott.

For example, the `test10st_codegen.thy` file uses Isabelle code generation to produce SML code to calculate the possible reductions of terms in the `test10st.ott` simply typed lambda calculus.

```
theory test10st_codegen
imports test10st_snapshot_out Executable_Set
begin

ML "reset Codegen.quiet_mode"

(* Code generation for the test10st simply typed lambda calculus. *)

constdefs
 ta :: t
"ta == (t_App (t_Lam ''z'' (t_Var ''z'')) (t_Lam ''y'' (t_Var ''y'')))"
;

code_module Test10st_codegen file "test10st_codegen.ml" contains
(*is_v
tsubst_T
tsubst_t*)
reduce_ta  = "(ta,_):reduce"


(* ...to build and demo the resulting test10st_codegen.ml code...

Isabelle test10st_codegen.thy
...‘use’ that...

...in a shell...
isabelle
use "test10st_codegen.ml";
open Test10st_codegen;

...a test term...
ta;
val it = t_App (t_Lam (["z"], t_Var ["z"]), t_Lam (["y"], t_Var ["y"]))

...a sample reduction...
DSeq.hd(reducep__1 ta);
val it = t_Lam (["y"], t_Var ["y"]) : Test10st_codegen.t

*)

end
```

19 Reference: Command-line usage

A good place to get started is one of the test `make` targets in the `ott` directory, e.g.

```
test10: tests/test10.ott
           bin/ott                                                \
                  -isabelle out.thy -coq out.v -hol outScript.sml \
                  -tex out.tex                                    \
                  -parse ":t:  (\z.z z) y"                        \
                  tests/test10.ott                                \
           && ($(LATEX) out; $(DVIPS) out -o)
```

When `make test10` is executed, `ott`:

- reads the source file `tests/test10.ott`
- prints on standard output various diagnostic information, including ASCII versions of the grammar and inductive definitions. By default these are coloured (using `vt220` control codes) with metavariables in red, nonterminals in yellow, terminals in green, and object variables in white. Scanning over this output quickly picks up some common errors.
- parses the symbolic term `(\z.z z) y` using the `t` grammar and prints the result to standard output
- generates Isabelle definitions in the file `out.thy`
- generates Coq definitions in the file `out.v`
- generates HOL definitions in the file `outScript.sml`
- generates a LaTeX document in the file `out.tex`, with a standard document preamble to make it self-contained.

That LaTeX document is then compiled and converted to postscript.

If multiple source files are specified then they are (after parsing) concatenated together.

The `%.out` `Makefile` target runs `ott` with common defaults on the file `%.ott`, so for example executing `make tests/test10.out` runs `ott` on `tests/test10.ott`, generating all outputs. There are also targets `%.coq.out`, `%.hol.out`, and `%.isa.out`, to generate just LaTeX and the code for one proof assistant, and `%.tex.out`, to generate just LaTeX.

The `ott` command-line options (with default values where applicable) are shown below.

```
Ott version 0.10.16   distribution of Mon Mar 9 14:53:23 GMT 2009

usage: ott <options> <filename> .. <filename>
  (use "OCAMLRUNPARAM=p  ott ..." to show the ocamlyacc trace)

  -tex <filename>                    Output TeX definitions
  -coq <filename>                    Output Coq definitions
  -hol <filename>                    Output HOL definitions
  -isabelle <filename>               Output Isabelle definitions
  -ocaml <filename>                  Output OCaml definitions
  -writesys <filename>               Output system definition
  -readsys <filename>                Input system definition
  -tex_filter <src><dst>             Files to TeX filter
  -coq_filter <src><dst>             Files to Coq filter
  -hol_filter <src><dst>             Files to HOL filter
  -isa_filter <src><dst>             Files to Isabelle filter
  -ocaml_filter <src><dst>           Files to OCaml filter
  -merge <false>                     merge grammar and definition rules
  -parse <string>                    Test parse symterm,eg ":nontermroot: term"
  -signal_parse_errors <false>       return >0 if there are bad defns
```

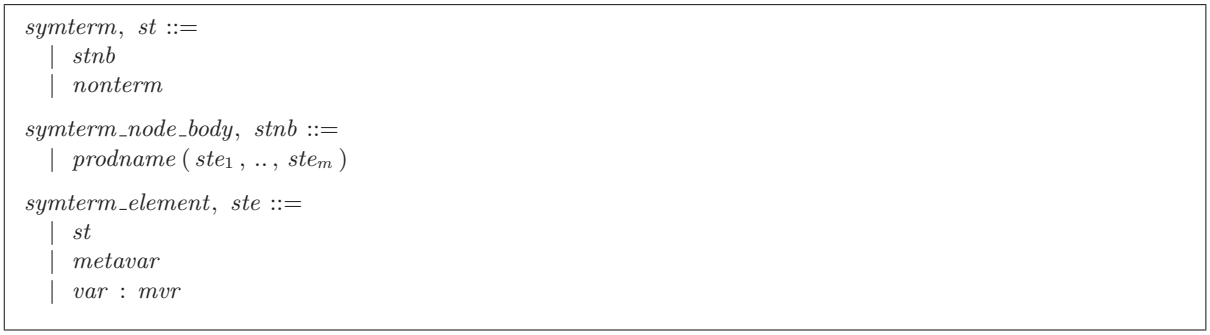

Figure 17: Mini-Ott in Ott: symbolic terms

```
-picky_multiple_parses <false>      Picky about multiple parses
-colour <true>                      Use (vt220) colour for ASCII pretty print
-show_pre_sort <false>              Show ASCII pre-sort pretty print syntax
-show_post_sort <false>             Show ASCII post-sort pretty print syntax
-show_defns <false>                 Show ASCII pretty print defns
-tex_show_meta <true>               Include meta prods and rules in TeX output
-tex_show_categories <false>        Signal production flags in TeX output
-tex_colour <true>                  Colour parse errors in TeX output
-tex_wrap <true>                    Wrap TeX output in document pre/postamble
-tex_name_prefix <string>           Prefix for tex commands (default "ott")
-isabelle_primrec <true>            Use "primrec" instead of "fun"
                                     for functions
-isabelle_inductive <true>          Use "inductive" instead of "inductive_set"
                                     for relations
-isa_syntax <false>                 Use fancy syntax in Isabelle output
-isa_generate_lemmas <false>        Lemmas for collapsed functions in Isabelle
-coq_avoid <1>                      coq type-name avoidance
                                     (0=nothing, 1=avoid, 2=secondaryify)
-coq_expand_list_types <true>       Expand list types in Coq output
-dot <filename>                     (debug) dot graph of syntax dependencies
-alltt <filename>                   (debug) alltt output of single source file
-sort <true>                        (debug) do topological sort
-process_defns <true>               (debug) process inductive reln definitions
-showraw <false>                    (debug) show raw grammar
-ugly <false>                       (debug) use ugly ASCII output
-coq_debug_expand <filename>        (debug) Tex definitions after Coq expand
-no_rbcatn <true>                   (debug) remove relevant bind clauses
-help                               Display this list of options
--help                              Display this list of options
```

20 Reference: The language of symbolic terms

A syntax definition conceptually defines two different languages: that of concrete terms of the object language, and that of symbolic terms over the object language. The former includes concrete variables (if nontrivial `lex` homs have been specified for metavariables). The latter includes the former but also allows symbolic metavariables and nonterminals. Symbolic terms may also include the production-name annotations mentioned in §3. For a syntax definition with list forms (c.f. §11) symbolic terms also include various list constructs. A simplified abstract syntax of symbolic terms is shown in Figure 17, omitting list forms. In this section we give an informal definition of the full concrete syntax of symbolic terms.

The premises and conclusions of inductive definition rules are symbolic terms. The language of symbolic terms is defined informally below, with interpretation functions $[\![\_]\!]$ that map defined entities into

grammar clauses.

For a rule *rule* =

$$nontermroot_1\ ..\ ,\ nontermroot_n\texttt{::''::=}\ prod_1\ ..\ prod_m$$

we have

$$\begin{array}{lll}[\![rule]\!] & ::= & \\ & | & nontermrootsuffix \quad (1)\\ & | & [\![prod_1]\!]\\ & | & ..\\ & | & [\![prod_m]\!]\end{array}$$

(1) for each *nontermroot* in the set $\{nontermroot_1\ ..\ ,\ nontermroot_n\}$ and for each *nontermroot* defined by any *rule*′ which is declared as a subrule of this rule.

For a production *prod* =

$$\texttt{|}\ element_1\ ..\ element_m\ \texttt{:::}\ prodname$$

we have

$$\begin{array}{lll}[\![prod]\!] & ::= & \\ & | & [\![element_1]\!]\ ..\ [\![element_m]\!]\\ & | & \texttt{:}prodname\texttt{:}\ [\![element_1]\!]\ ..\ [\![element_m]\!]\end{array}$$

For an element there are various cases.

1. For a terminal *terminal*

$$[\![terminal]\!] \quad ::= \quad terminal$$

2. For a nonterminal *nontermroot suffix*

$$[\![nontermroot\ suffix]\!] \quad ::= \quad [\![rule]\!]$$

   where *rule* includes *nontermroot* among the nonterminal roots it defines. (Note that this does not depend on what *suffix* was used in the grammar, and similarly for the *metavar* case below.)

3. For an index variable *indexvarroot*

$$[\![indexvarroot]\!] \quad ::= \quad indexvarroot'$$

   for each *indexvarroot*′ defined by the `indexvar` definition that defines *indexvarroot*.

4. For a metavariable *metavarroot suffix*

$$\begin{array}{lll}[\![metavarroot\ suffix]\!] & ::= & \\ & | & metavarroot'\text{suffix} \quad (1)\\ & | & variable\end{array}$$

   (1) for each *metavarroot*′ defined by the `metavar` definition that defines *metavarroot*. (2) where *variable* ranges over all the strings defined by the `lex` regexp of the `metavar` definition that defines *metavarroot*, except for any string which can be parsed as a nonterminal, metavariable or terminal of the syntax definition.

5. A list form element *element* could be any of the following, either without a separating terminal:

$$\begin{array}{l}element_1..element_n\ dots\ element'_1..element'_n\\ \texttt{</}\ element_1..element_n\ \texttt{//}\ indexvar\ \texttt{/>}\\ \texttt{</}\ element_1..element_n\ \texttt{//}\ indexvar\ \texttt{IN}\ indexvar'\ \texttt{/>}\\ \texttt{</}\ element_1..element_n\ \texttt{//}\ indexvar\ \texttt{IN}\ number\ dots\ indexvar'\ \texttt{/>}\\ \texttt{</}\ element_1..element_n\ \texttt{//}\ indexvar\ \texttt{IN}\ number\ dots\ indexvar'\texttt{-1}\ \texttt{/>}\end{array}$$

   or with a separating terminal:

$$\begin{array}{l}element_1..element_n\ terminal\ dots\ terminal\ element'_1..element'_n\\ \texttt{</}\ element_1..element_n\ \texttt{//}\ terminal\ \texttt{//}\ indexvar\ \texttt{/>}\\ \texttt{</}\ element_1..element_n\ \texttt{//}\ terminal\ \texttt{//}\ indexvar\ \texttt{IN}\ indexvar'\ \texttt{/>}\\ \texttt{</}\ element_1..element_n\ \texttt{//}\ terminal\ \texttt{//}\ indexvar\ \texttt{IN}\ number\ dots\ indexvar'\ \texttt{/>}\\ \texttt{</}\ element_1..element_n\ \texttt{//}\ terminal\ \texttt{//}\ indexvar\ \texttt{IN}\ number\ dots\ indexvar'\texttt{-1}\ \texttt{/>}\end{array}$$

In any of these cases the interpretation $[\![element]\!]$ is the lists (separated by the *terminal* if one was specified) of concrete list entries and of list forms. Without a separating *terminal*, this is:

$$
\begin{array}{lll}
[\![element]\!] & ::= & (\text{concrete\_list\_entry}|\text{list\_form})^* \qquad (2),(3) \\
\\
\text{concrete\_list\_entry} & ::= & [\![element_1]\!] \,..\, [\![element_n]\!] \\
\\
\text{list\_form} & ::= & \\
 & | & [\![element_1]\!] \,..\, [\![element_n]\!]\ dots'\ [\![element'_1]\!] \,..\, [\![element'_n]\!] \qquad (1) \\
 & | & \texttt{</}\ [\![element_1]\!] \texttt{..}[\![element_n]\!]\ \texttt{//}\ indexvar''\ \texttt{/>} \\
 & | & \texttt{</}\ [\![element_1]\!] \texttt{..}[\![element_n]\!]\ \texttt{//}\ indexvar''\ \texttt{IN}\ indexvar'''\ \texttt{/>} \\
 & | & \texttt{</}\ [\![element_1]\!] \texttt{..}[\![element_n]\!]\ \texttt{//}\ indexvar''\ \texttt{IN}\ number'\ dots'\ indexvar'''\ \texttt{/>} \\
 & | & \texttt{</}\ [\![element_1]\!] \texttt{..}[\![element_n]\!]\ \texttt{//}\ indexvar''\ \texttt{IN}\ number'\ dots'\ indexvar'''\texttt{-1}\ \texttt{/>}
\end{array}
$$

This is subject to constraints: (1) that $[\![element_1]\!] \,..\, [\![element_n]\!]$ and $[\![element'_1]\!] \,..\, [\![element'_n]\!]$ can be anti-unified with exactly one varying index; (2) if the list has only concrete entries (i.e., no list forms), its length must meet the constraint of any dots in the *element*.

With a separating *terminal*, we have:

$$[\![element]\!] \quad ::= \quad \epsilon|(\text{concrete\_list\_entry}|\text{list\_form})(terminal(\text{concrete\_list\_entry}|\text{list\_form}))^*$$

In the above

$$
\begin{array}{lll}
\text{dots} & ::= & \texttt{..}|\texttt{...}|\texttt{....} \\
\text{number} & ::= & \texttt{0}|\texttt{1} \\
\text{suffix} & ::= & \text{suffix\_item}^* \\
\text{suffix\_item} & ::= & \\
 & | & (\texttt{0}|\texttt{1}|\texttt{2}|\texttt{3}|\texttt{4}|\texttt{5}|\texttt{6}|\texttt{7}|\texttt{8}|\texttt{9})^+ \quad \text{(longest match)} \\
 & | & \texttt{\_} \\
 & | & \texttt{'} \\
 & | & indexvar \\
 & | & indexvar\texttt{-1}
\end{array}
$$

Further, whitespace (`' '|'\010'|'\009'|'\013'|'\012'`) is allowed before any token except a those in a suffix, and nonterminals, metavariables, index variables, and terminals that end with an alphanumeric character, must not be followed by an alphanumeric character.

The tool also builds a parser for concrete terms, with fake nonterminal roots `concrete_ntr` for each primary `ntr` of the syntax definition. One can switch to concrete-term parsing with a `:concrete:` annotation, as in the example

```
\[ [[ :concrete: \Z1<:Top. \x:Z1.x ]]\]
```

shown in Figure 10. Below such an annotation, only concrete terms are permitted, with no further annotation, no symbolic nonterminals or metavariables, no list dot forms or comprehensions, etc.

Parsing of terms is done with a scannerless GLR parser over character-list inputs. The parser searches for all parses of the input. If none are found, the ASCII and TeX output are annotated `no parses`, with a copy of the input with `***` inserted at the point where the last token was read. This is often at the point of the error (though if, for example, a putative dot form is read but the two element lists cannot be anti-unified, it will be after the point of the error). If multiple parses are found, the TeX output is annotated `multiple parses` and the different parses are output to the console in detail during the Ott run.

The GLR parser achieves reasonable performance on the small symbolic terms that are typical in semantic rules. Its performance on large (whole-program size) examples is untested.

21 Reference: Generation of proof assistant definitions

This section briefly summarises the steps involved in the generation of proof assistant definitions from an Ott source file. For a description of the locally-nameless backend, refer to `http://moscova.inria.fr/ zappa/projects/ln_o`

21.1 Generation of types

- The primary metavariable roots and primary nonterminal roots are used directly as the names of proof assistant types, except where they have a hom specifying a root-overriding string.
- Type abbreviation declarations are produced for metavars, in the source-file order, skipping metavars defined as `phantom`.
- Type generation considers each rule of the user's source grammar except those for `formula` and `terminals` (or the synthesized rules for the syntax of judgements or `user_syntax`).
- The subrule order is analysed to identify the top elements. For each of those, a proof assistant type will be generated — either a free type (`coq: inductive`, `isa: datatype`, `hol: Hol_datatype`), or if there is a type hom for the proof assistant in question, a type abbreviation. No types are generated for the non-top elements, as they will be represented as predicates over the top free type above them.
- For the former, each non-meta production of the rule gives rise to a constructor. The production name (with any per-rule prefix already applied) is used directly as the constructor name. The (curried) constructor argument types are taken from the types associated with the metavariables and nonterminals mentioned in the production body.
- Rules are topologically sorted according to the dependency order (a free-type rule directly depends on another if one of its non-meta productions includes a nonterminal of the other; dependencies for rules with a type-hom for the proof assistant in question are obtained from a crude lexing of the body of the type hom). We then generate mutually recursive type definitions for connected components, in an order consistent with the dependencies.
- For productions that involve list dot forms or list comprehension forms, for HOL and Isabelle we produce constructors with argument types that involve native list types. For Coq, however, we synthesise an additional inductive type for each list-of-tuples that arises (both for those that occur in the grammar and for others required in the translations of inductive definitions) and include them in the topological sort.

21.2 Generation of functions

A small number of library functions (`list_mem`, `list_minus`,...) are included in the output if they are required.

Several Coq list functions (`map`, `make`, `unmake`, `nth`, `app`) are generated for each synthesized list type.

The definitions of the more interesting functions (subrule predicates, binding auxiliaries, free variable functions, and substitutions) are generated over the free types generated for the maximal elements of the subrule order (generation of these functions for rules with type homs is not supported). The definitions are by pattern-matching and recursion. The patterns are generated by building canonical symbolic terms from the productions of each relevant rule. The recursion is essentially primitive recursion: for Coq we produce `Fixpoint`s or `Definition`s (the latter is sometimes needed as the former gives an error in the case where there is no recursion); for Isabelle we produce `primrec`s (or, experimentally, `fun`s); for HOL we use an `ottDefine` variant of the `Define` package. In general we have to deal both with the type dependency (the topologically sorted mutually recursive types described above) and with function dependency — for example, for subrule predicates and binding auxiliaries we may have multiple mutually recursive functions over the same type.

For Coq the function generation over productions that involve list types must mirror that, so we generate auxiliary functions that recurse over those list types.

For Isabelle the `primrec` package does not support definitions involving several mutually recursive functions over the same type, so for these we generate single functions calculating tuples of results, define the intended functions as projections of these, and generate lemmas (and simple proof scripts) characterising them in terms of the intended definitions. Further, it does not support pattern matching involving nested constructors. We therefore generate auxiliary functions for productions with embedded list types.

Isabelle tuples are treated as iterated pairs, so we do the same for productions with tuples of size 3 or more. Isabelle also requires a function definition for each recursive type. In the case where there are multiple uses of the same type (e.g. several uses of `t list` in different productions) all the functions we wish to generate need identical auxiliaries. As yet, the tool does not generate the identical copies required.

If the option `-isabelle_primrec` is set to `false`, then Ott uses the `fun` package instead of the `primrec` package. Since at the time of writing Isabelle 2008 is not capable of proving automatically termination of all the `fun`s that Ott generates, this feature should be considered experimental.

For HOL the standard `Define` package tries an automatic termination proof. For productions that involve list types our generated functions involve various list functions which prevent those proofs working in all cases. We therefore use an `ottDefine` variant (due to Scott Owens), with slightly stronger support for proving termination of definitions involving list operators.

21.2.1 Subrule predicates

We generate subrule predicates to carve out the subsets of each free proof assistant type (from the maximal elements of the subrule order) that represent the rules of the grammar. The non-free rules are the least subset of the rules that either (1) occur on the left of a subrule (`<::`) declaration, or (2) have a (non-meta) production that mentions a non-free rule. Note that these can include rules that are maximal elements of the subrule order, e.g. if an expression grammar included a production involving packaged values. The subrule predicate for a type is defined by pattern matching over constructors of the maximal type above it — for each non-meta production of the maximal type it calculates a disjunction over all the productions of the lower type that are subproductions of it, invoking other subrule predicates as appropriate.

21.2.2 Binding auxiliaries

The binding auxiliary functions calculate the intuitive semantics of auxiliary functions defined in bindspecs of the Ott source file. Currently these are represented as proof assistant lists of metavariables or nonterminals (arguably set types should be used instead, at least in Isabelle).

21.2.3 Free variables

The free variable functions simply walk over the structure of the free proof assistant types, using any bind specifications (and binding auxiliaries) as appropriate. For these, and for substitutions, we simplify the generated functions by using the dependency analysis of the syntax to exclude recursive calls where there is no dependency.

21.2.4 Substitutions

The generated substitution functions also walk over the structure of the free proof assistant types. For each production, for each occurrence of a nonterminal `nt` within it, we first calculate the things (of whatever type is in question) binding in that `nt`, i.e. those that should be removed from the domain of any substitution pushed down into it. There are two cases: (1) the `mse'` from any `bind mse' in nt`; (2) `nt` itself if it occurs in the `mse''` of any `bind mse'' in nt''`, i.e. `nt` itself if it is directly used to bind elsewhere. List forms within bindspecs are dealt with analogously.

The substitution function clause for a production is then of one of two forms: either (1) the production comprises a single element, of the nonterminal or metavariable that we are substituting for, and this is within the rule of the nonterminal that it is being replaced by, or (2) all other cases. For (1) the element is compared with the domain of the substitution, and replaced by the corresponding value from the range if it is found. For (2) the substitution functions are mapped over the subelements, having first removed any bound things from the domain of the substitution.

This is all done similarly, but with differences in detail, for single and for multiple substitutions.

21.3 Generation of relations

The semantic relations are defined with the proof-assistant inductive relations packages (`coq`: `Inductive`, `isa`: `inductive`, `hol`: `Hol_reln`). They use the mutual recursion structure that is given by the user, with each `defns` block giving rise to a potentially mutually recursive definition of each `defn` inside it. (It is debatable whether it would be preferable to do an automatic dependency analysis and topological sort, as for the syntax.) Each definition rule gives rise to an implicational clause, essentially that the premises (Ott `formulas`) imply the conclusion (an Ott symbolic term of whichever judgement is being defined). In addition:

- Symbolic terms are transformed in various different ways:
  - Nodes of non-meta productions are output as applications of the appropriate proof-assistant constructor (and, for a subrule, promoted to the corresponding constructor of a maximal rule).
  - Nodes of meta productions are transformed with the user-specified homomorphism.
  - Nodes of judgement forms are represented as applications of the defined relation in Coq and HOL, and as set-membership assertions in Isabelle.
  - Lists of formulae (the `formula_dots` production) are special-cased.
- For each nonterminal of a non-free syntax rule (as in §21.2.1) that occurs, e.g. a usage of `v'` where `v<::t`, an additional premise invoking the subrule predicate for the non-free rule is added, e.g. `is_v v'`.
- The set of symbolic terms of the definition rule are analysed together to identify list forms with the same bounds. A single proof assistant variable is introduced for each such, with appropriate projections and list maps/foralls at the usage points.
- For Coq, auxiliary defined relations are introduced for list forms.
- For Coq, as the projections from list forms involve (Ott-generated) `nth` functions that return option types, for any such projection a pattern-match against `Some` is introduced as an additional premise.
- For Coq and HOL, explicit quantifiers are introduced for all variables mentioned in the rule.

22 Reference: Summary of homomorphisms

Homomorphisms can appear in various positions in an Ott source file. The table below summarises their meanings. A $\surd$ indicates that arguments are meaningful for that usage (e.g. `[[e1]]` in a production mentioning a nonterminal or metavariable `e1`).

	a metavar or indexvar declaration, after one of the defined metavar/indexvar roots, or a rule, after one of the defined nonterminal roots	
tex	$\surd$	LaTeX typesetting for symbolic variables with that root
isa/**coq**/**hol**/**ocaml**		Isabelle/Coq/HOL/OCaml root overriding string (1)

a metavar or indexvar declaration, after the `::=`

isa		Isabelle representation type
coq		Coq representation type
hol		HOL representation type
ocaml		OCaml representation type
tex	√	LaTeX typesetting for symbolic variables
com		comment to appear in LaTeX syntax definition
coq-equality		Coq proof script to decide equality over the representation type
repr-locally-nameless		(Coq only) use a locally-nameless representation
phantom		do not generate the representation type in theorem prouver output
lex		regular expression for lexing concrete variables
texvar	√	LaTeX typesetting for concrete variables
isavar	√	Isabelle output for concrete variables
holvar	√	HOL output for concrete variables
ocamlvar	√	OCaml output for concrete variables

a rule, after the `::=`

isa		Isabelle representation type, if a non-free type is required
coq		Coq representation type, if a non-free type is required
hol		HOL representation type, if a non-free type is required
ocaml		OCaml representation type, if a non-free type is required
tex	√	LaTeX typesetting for symbolic variables
com	√	comment to appear in LaTeX syntax definition
coq-equality		Coq proof script to decide equality over the representation type
ich	√	shorthand for identical **coq**, **isa** and **hol** homs
ic	√	shorthand for identical **coq** and **isa** homs
ch	√	shorthand for identical **coq** and **hol** homs
ih	√	shorthand for identical **isa** and **hol** homs

a production

isa	√	Isabelle output, for a non-free (meta) production
coq	√	Coq output, for a non-free (meta) production
hol	√	HOL output, for a non-free (meta) production
ocaml	√	OCaml output, for a non-free (meta) production
tex	√	LaTeX typesetting for symbolic terms
com	√	comment to appear in LaTeX syntax definition
isasyn	√	Isabelle mixfix syntax output
isaprec		Isabelle mixfix syntax precedence string
ich	√	shorthand for identical **coq**, **isa** and **hol**homs
ic	√	shorthand for identical **coq** and **isa** homs
ch	√	shorthand for identical **coq** and **hol** homs
ih	√	shorthand for identical **isa** and **hol** homs

a production of the `terminals` grammar

isa		Isabelle output, for terminals in default generated Isabelle mixfix declarations
tex		LaTeX default typesetting for terms
com	√	comment to appear in LaTeX syntax definition

a **defn**, before the **by**

tex	√	LaTeX typesetting for symbolic terms
com	√	comment to appear in LaTeX syntax definition
isasyn	√	Isabelle mixfix syntax output
isaprec		Isabelle mixfix syntax precedence string

a `homs` section clause (for a production or a definition)

as in the above production and **defn** forms

an **embed** section

isa	embedded Isabelle output, appearing either as preamble, before defns, or postamble
coq	embedded Coq output, appearing either as preamble, before defns, or postamblea
hol	embedded HOL output, appearing either as preamble, before defns, or postamble
ocaml	embedded OCaml output, appearing either as preamble, before defns, or postamble
tex	embedded LaTeX output, appearing either as preamble, before defns, or postamble

(1) This is occasionally useful to work around a clash between a metavar or nonterminal primary root and a proof assistant symbol, e.g. `value` in Isabelle or `T` in HOL.

23 Reference: The Ott source grammar

This is automatically generated (by `mly-y2l`) from the `ocamlyacc` grammar for Ott.

The lexing of Ott source files is context-dependent; this does not show that.

Not everything in the grammar is fully supported — in particular, option element forms, non-dotted element list forms, the three `names` distinctness forms of bindspecs, and context rules.

24 Reference: Examples

The project web page

```
http://www.cl.cam.ac.uk/users/pes20/ott/
```

gives a variety of examples. Some of these, and additional small examples, are included in the distribution in the `tests` directory. Typically they can be built using the `Makefile` in the `ott` directory, e.g. typing `make test10` or (more generally) `make tests/test10.out`) there.

`test10.ott`	untyped CBV lambda
`test10st.ott`	simply typed CBV lambda
`test8.ott`	ML polymorphism example
`test7a.ott`	POPLmark Fsub example (without records)
`test7b.ott`	POPLmark Fsub example (with records)
`leroy-jfp96.ott`	Leroy module system
`lj.ott`	LJ: Lightweight Java
`test7t.mng`	whole-document tex mng source (`make test7afilter` to build)
`test7tt.mng`	fragment tex mng source
`test11.ott`	subrule example
`test12.ott`	topological sort example
`test13.ott`	small bindspec fragment
`test10st_snapshot_out.thy`	snapshot of generated Isabelle from `test10st.ott`
`test10st_metatheory_autoed.thy`	Isabelle proof script for type preservation and progress
`test10st_codegen.thy`	Isabelle code generation script for reduction
`test10_isasyn.ott`	Isabelle mixfix syntax example
`test10st_metatheoryScript.sml`	HOL proof script for type preservation and progress
`test17.10.ott`	list comprehension examples

The `examples/tapl` directory contains several examples taken from the book 'Types and Programming Languages' by Benjamin Pierce. The `make` targets, listed below, combine Ott source files following roughly the TinkerType component structure used in TAPL.

`sys-bool`	booleans (p34)
`sys-arith`	arithmetic expressions (p41)
`sys-untyped`	untyped lambda-calculus with booleans
`sys-puresimple`	simply-typed lambda-calculus
`sys-tybool`	typed booleans
`sys-tuple`	
`sys-sortoffullsimple`	
`sys-roughlyfullsimple`	
`sys-puresub`	
`sys-purercdsub`	

Other examples can be found on the locally-nameless backend web page.

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